

PSD

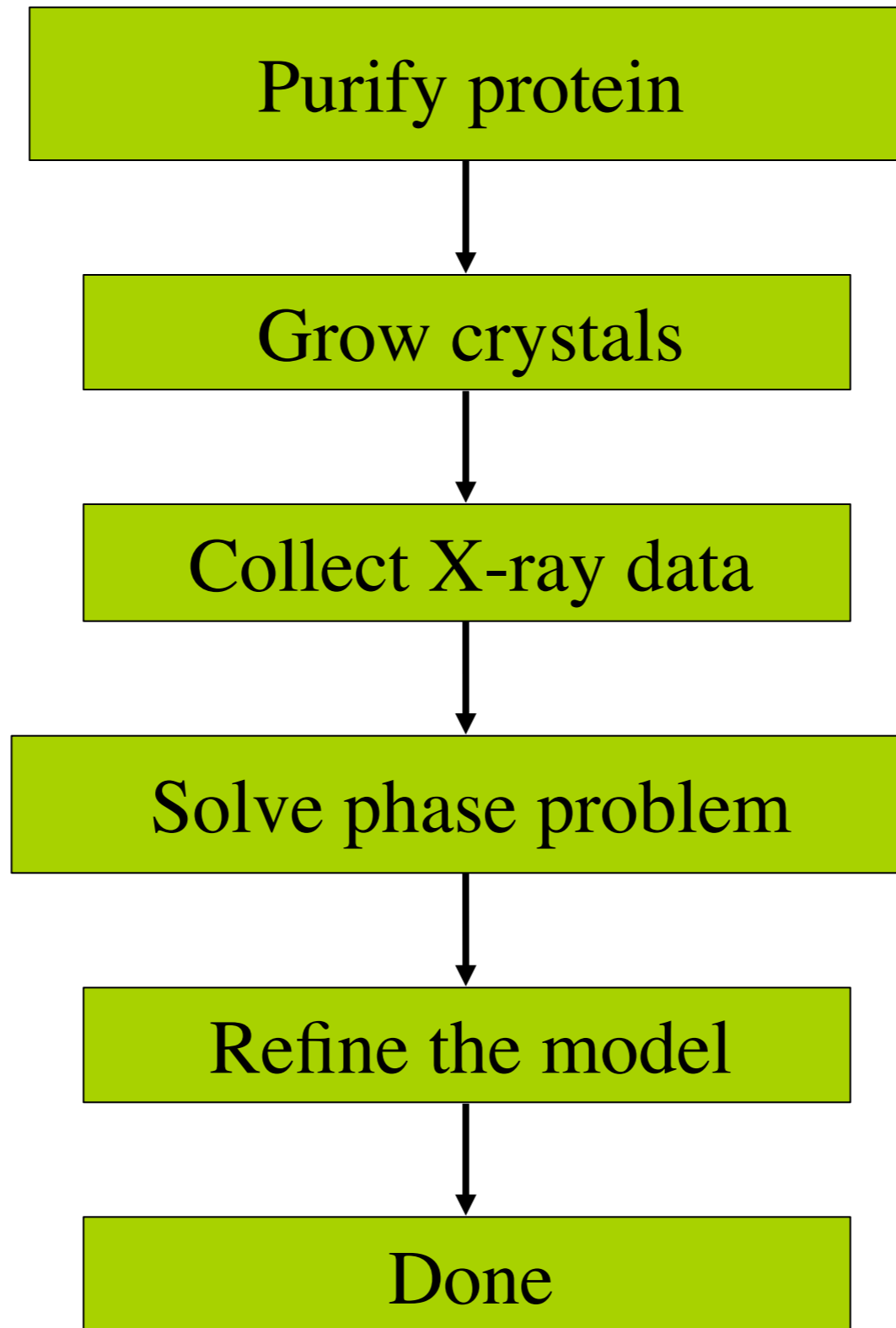
# Xray lecture 13

Overview

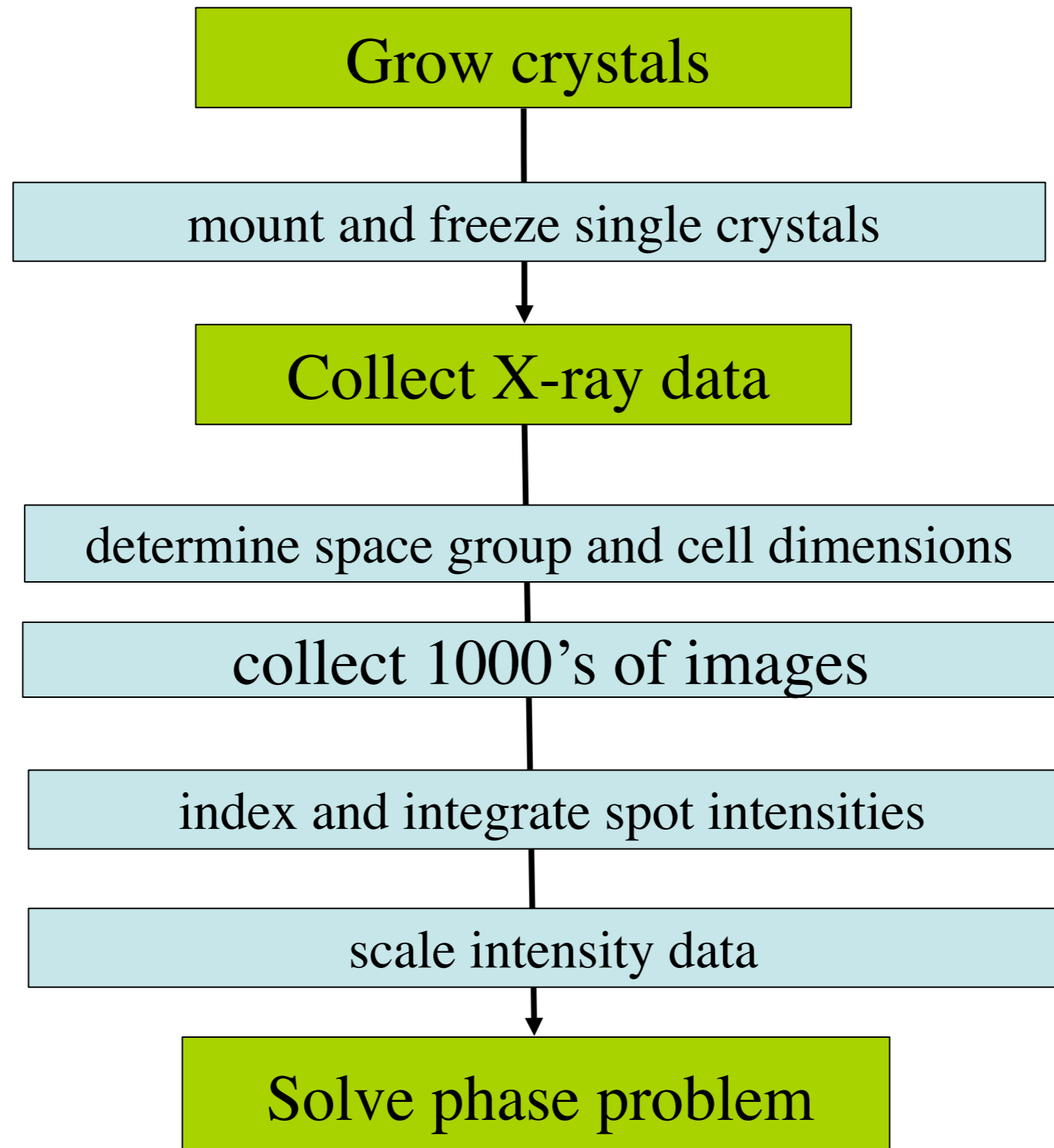
Laue photography

X-ray laser femtosecond Laue photography

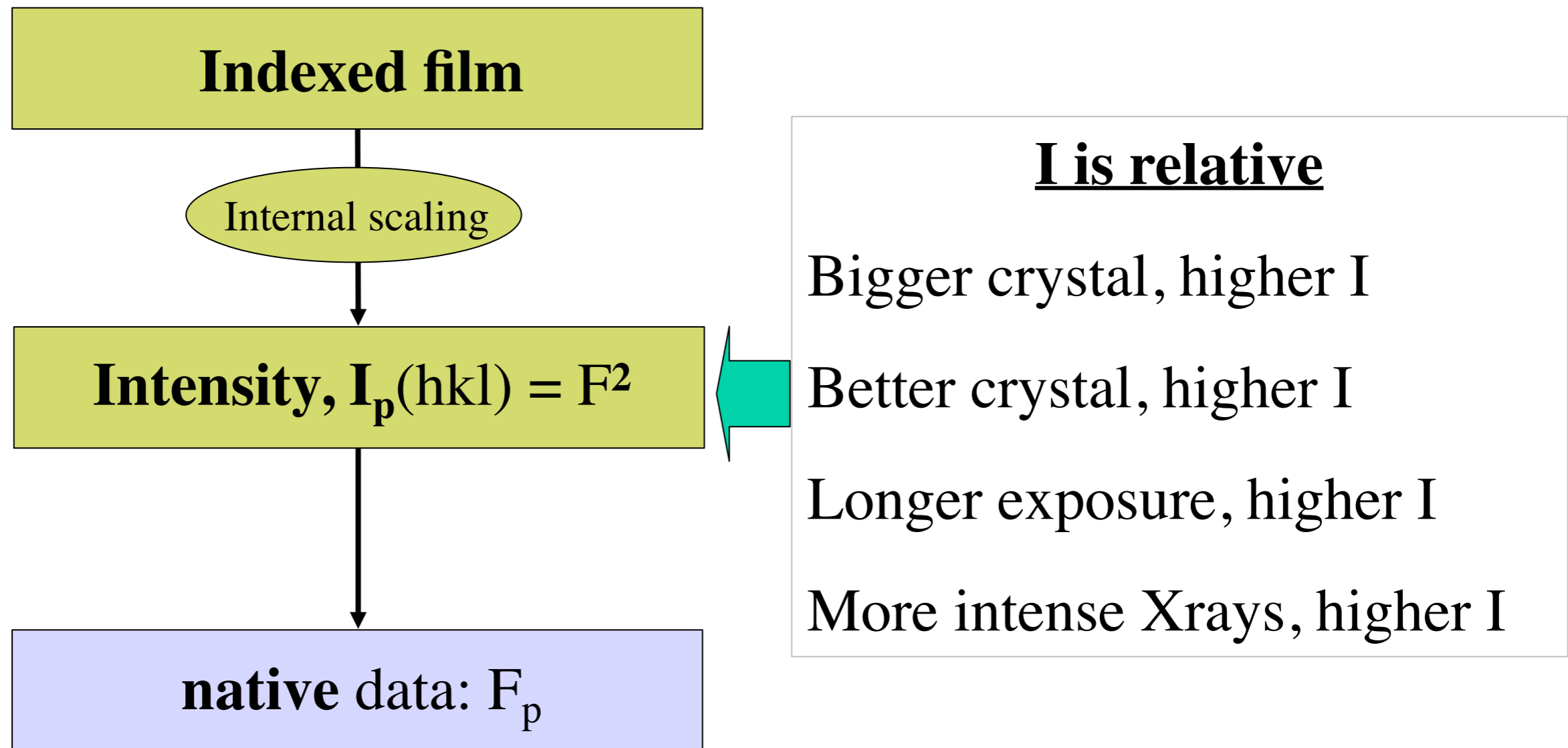
# From protein to protein structure



# From protein to phasing



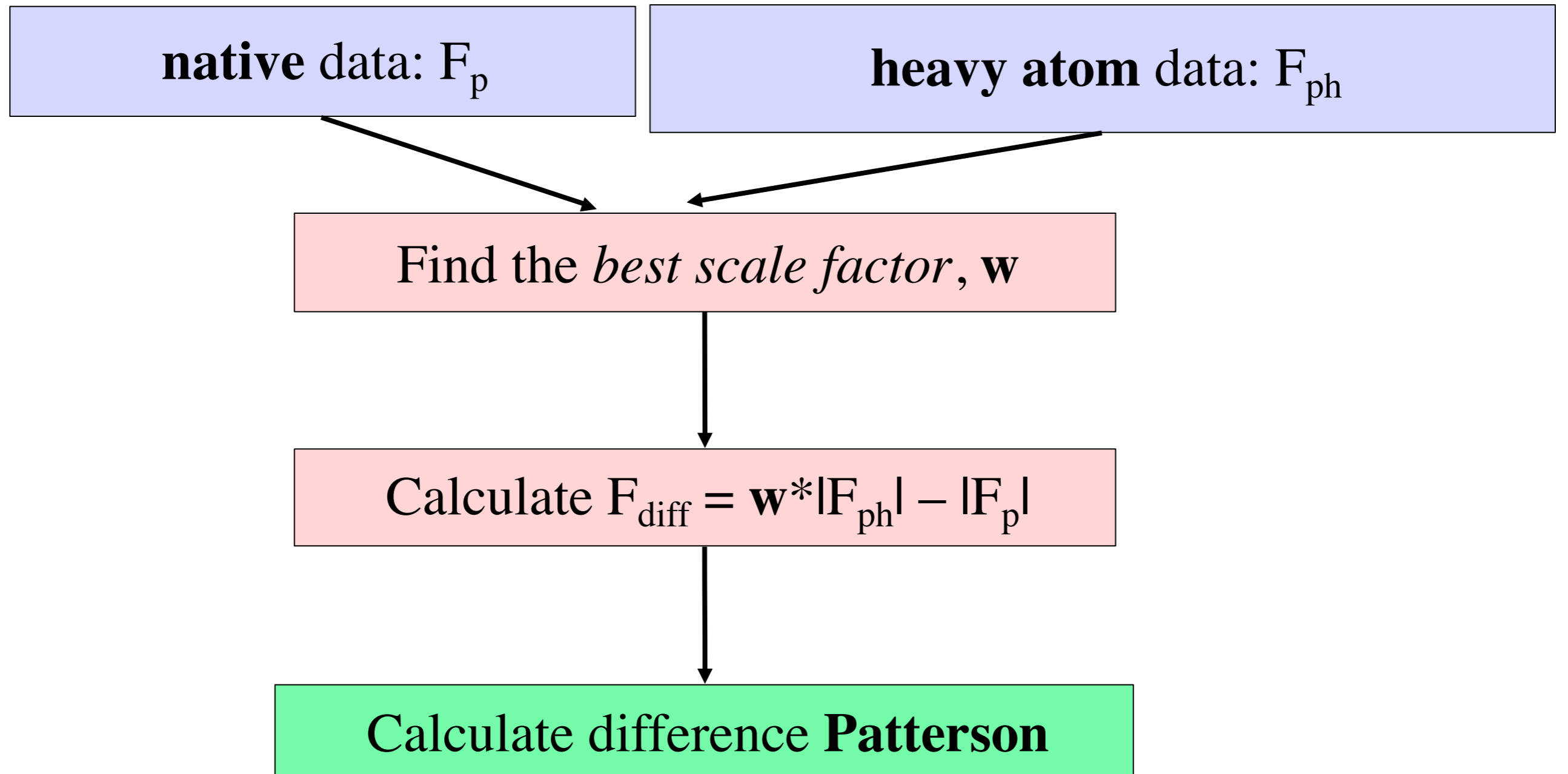
# From crystal to data



Because there is no absolute scale:

$F_p$  and  $F_{ph}$  are on *different scales*

# From data to Patterson map



# From data to **phases**

**native data:**  $F_p$

**heavy atom data:**  $F_{ph}$

Calculate difference **Patterson**

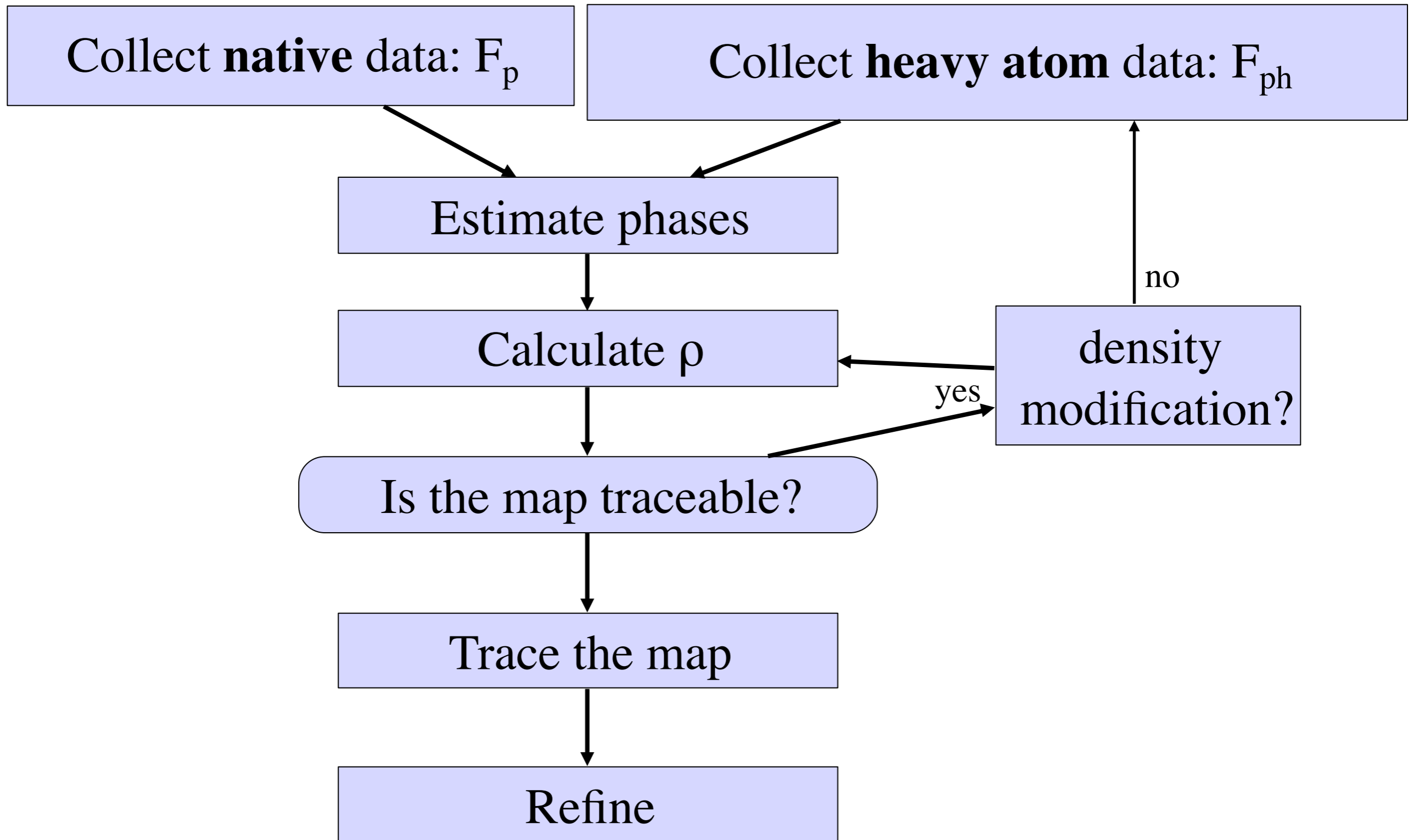
Find heavy atom **peaks** on Harker sections

Solve for heavy atom positions using symmetry

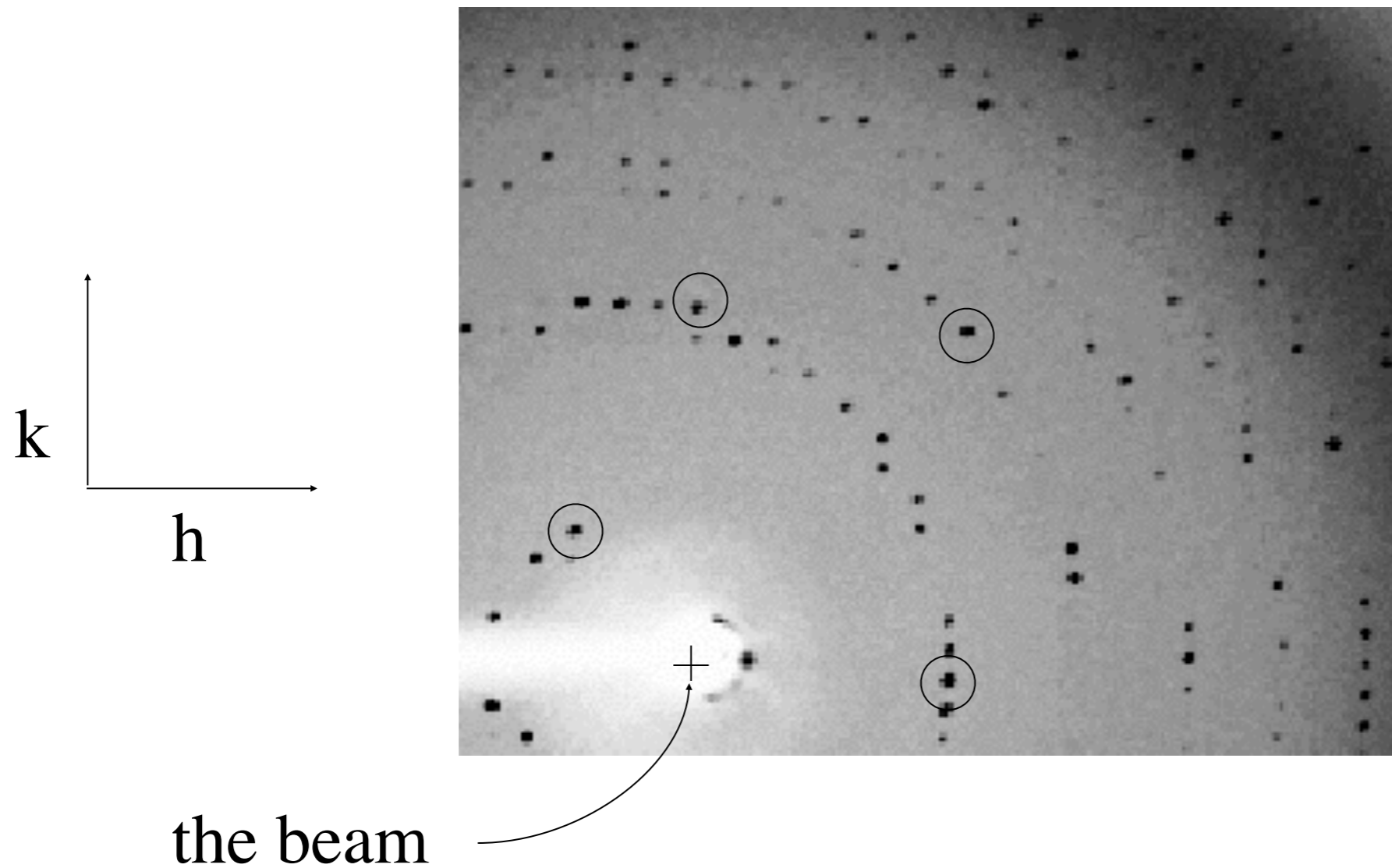
Calculate heavy atom vectors

Estimate phases

# From data to model



# In class exercise: index these spots





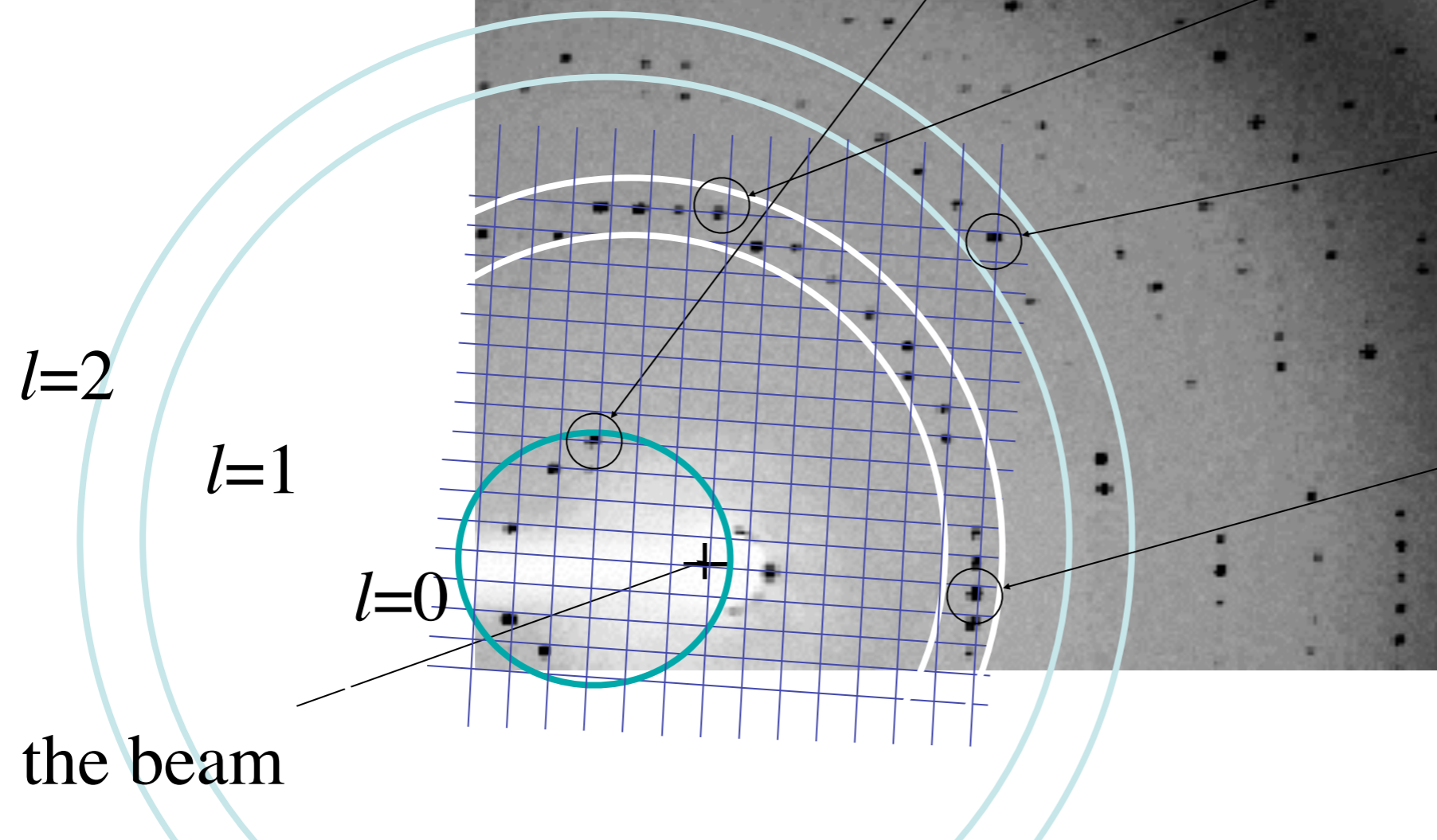
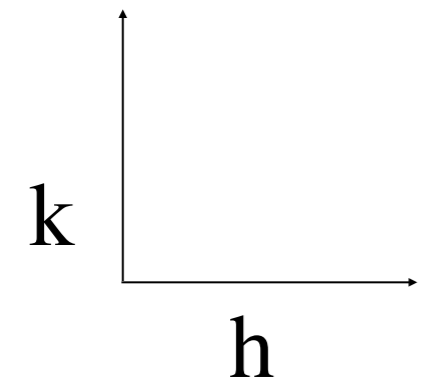
answer

hkl =  $\bar{3}$  4 0

0 12 1

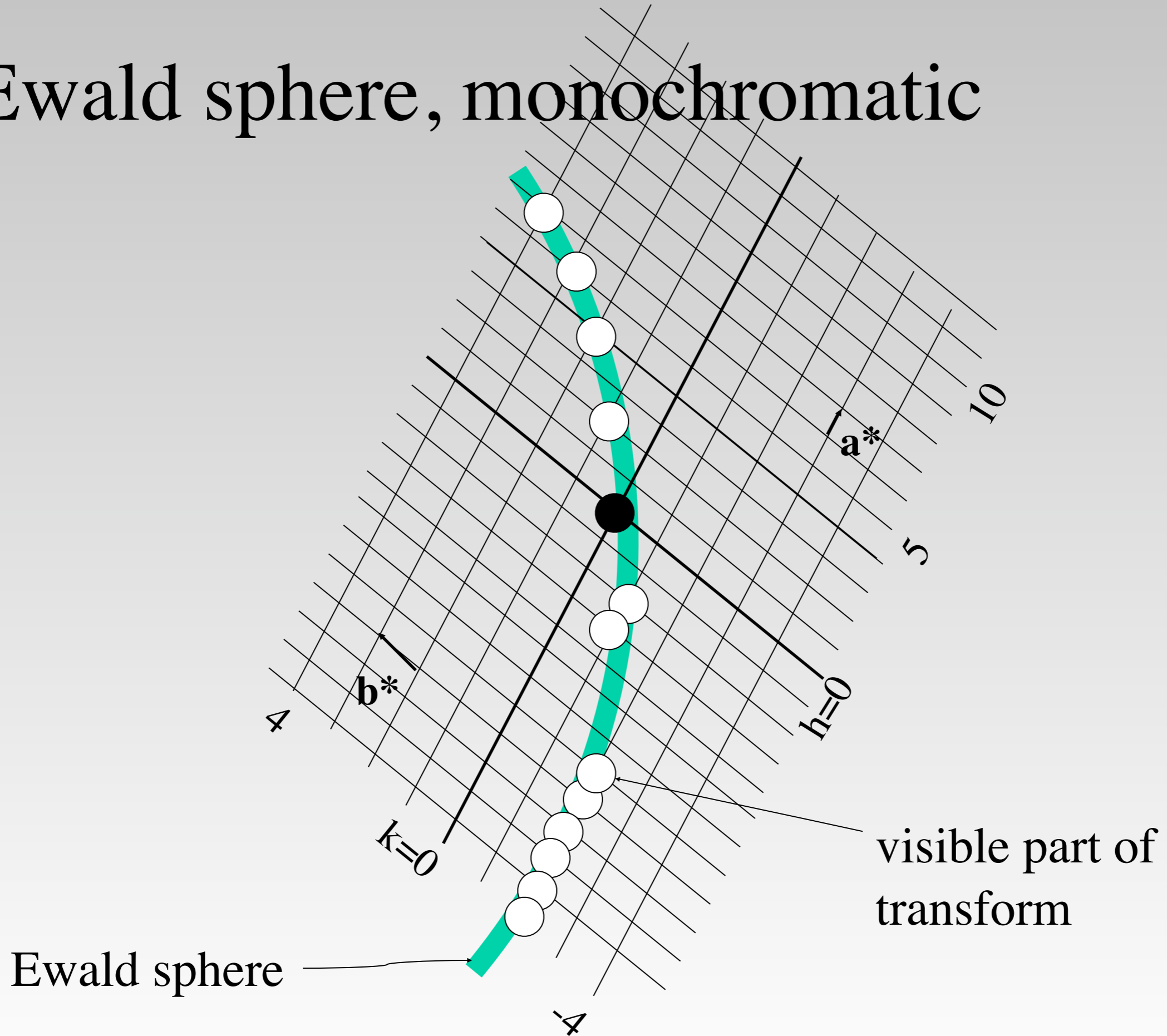
7 12 2

7 0 1



the beam

# Ewald sphere, monochromatic



# Laue Photography

Mathematics

Structures

time-resolved crystallography

neutron crystallography

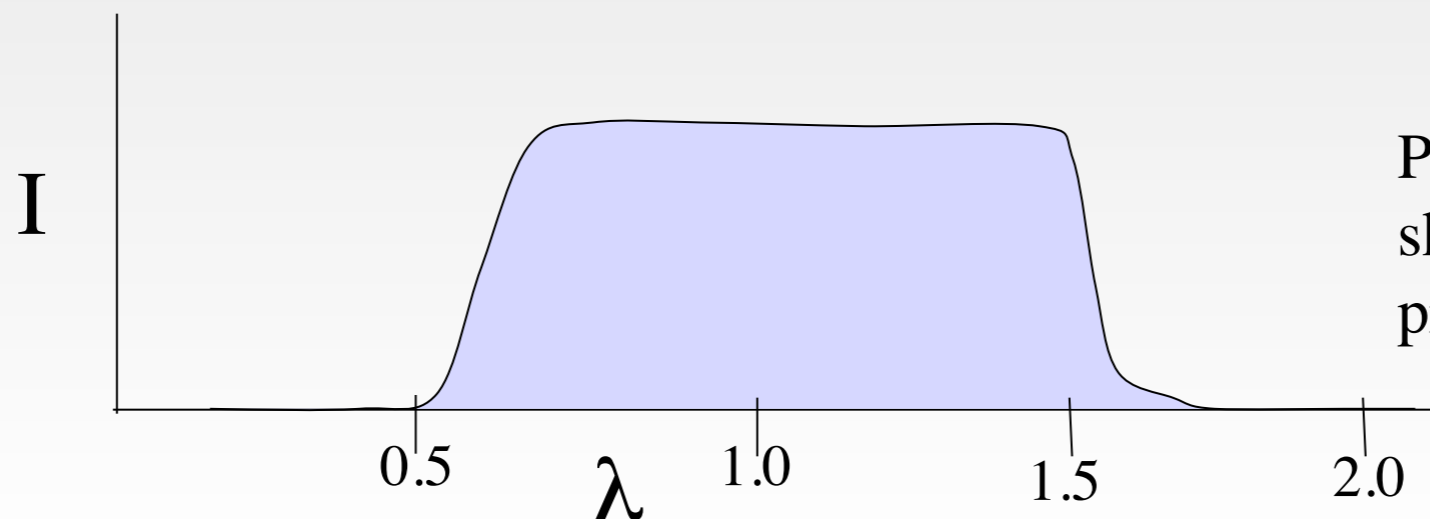
electron crystallography

X-ray free electron laser

nanocrystallography

# Laue Method

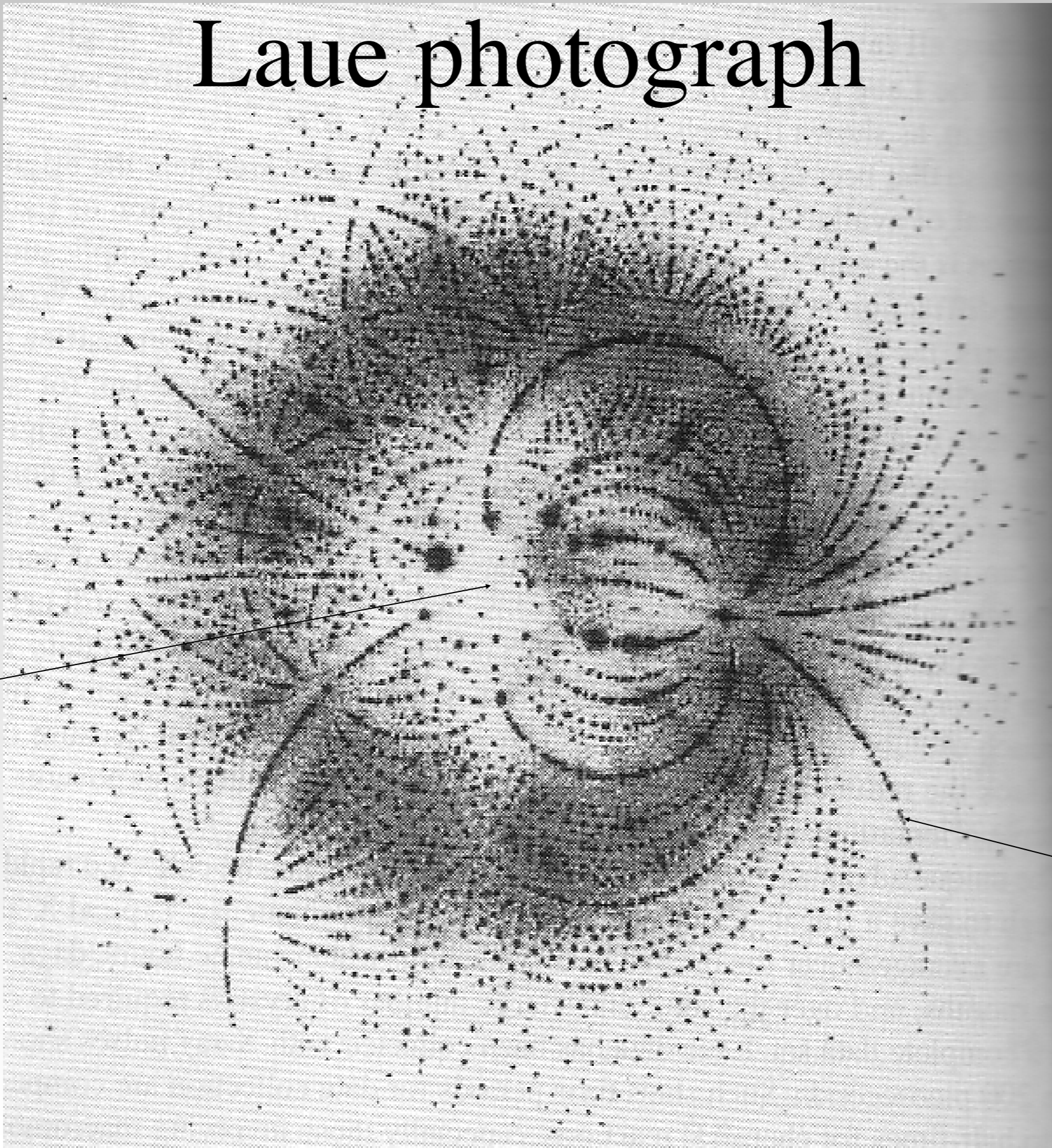
- Uses polychromatic (“white”) X-rays. (generally  $\lambda < 2.0 \text{ \AA}$ )
- Allows data to be collected ultra-fast, leading to its application in “time-resolved” crystallography.
- Still photographs cover a wide range of reciprocal space. A whole dataset may be collected on a few films.
- Requires synchrotron radiation



Polychromatic X-rays should have a flat intensity profile.

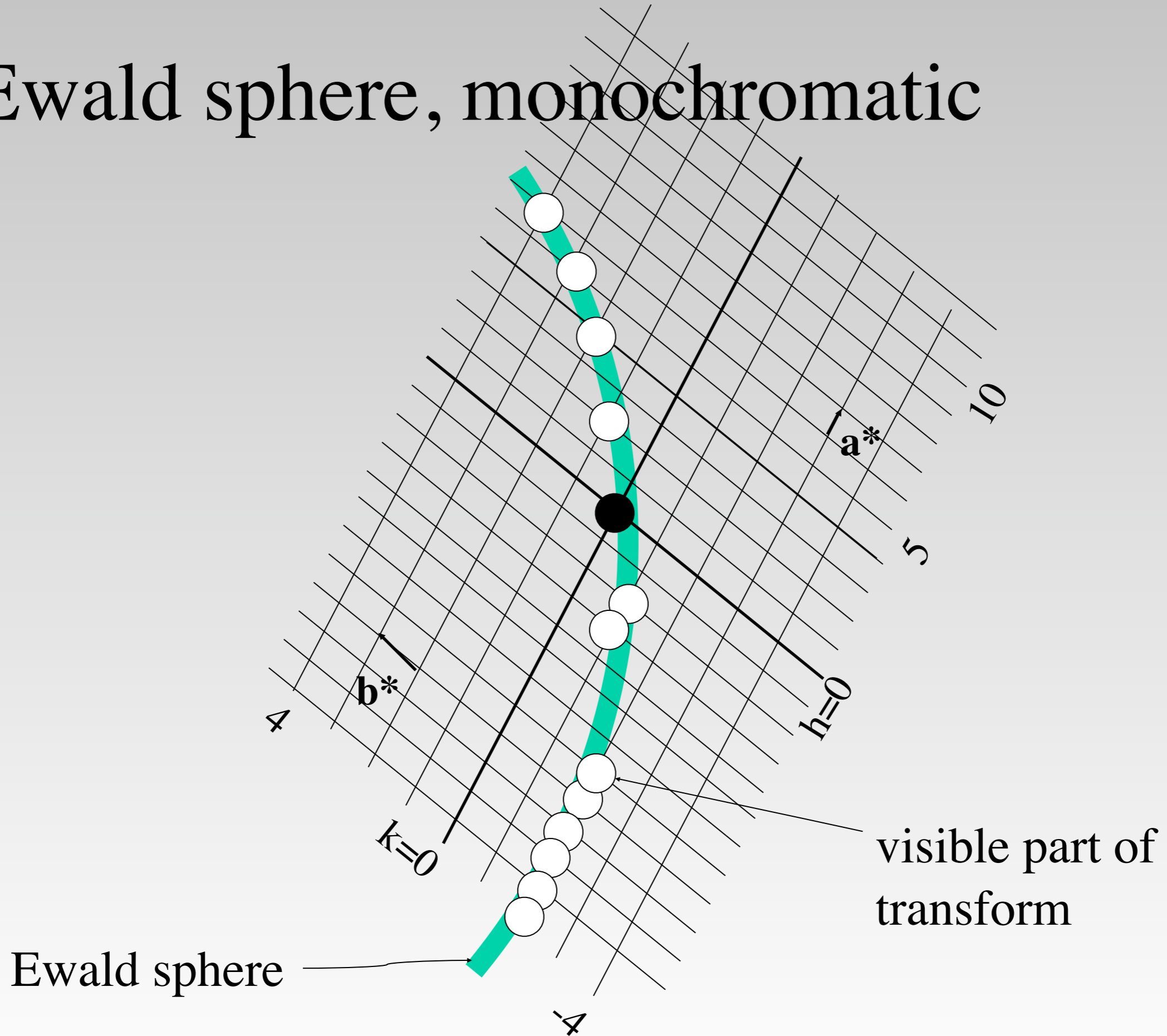
# Laue photograph

beam



**Note:** Very small separation between spots. This means the crystals must be small, the beam must be small, and the crystals must be well-ordered.

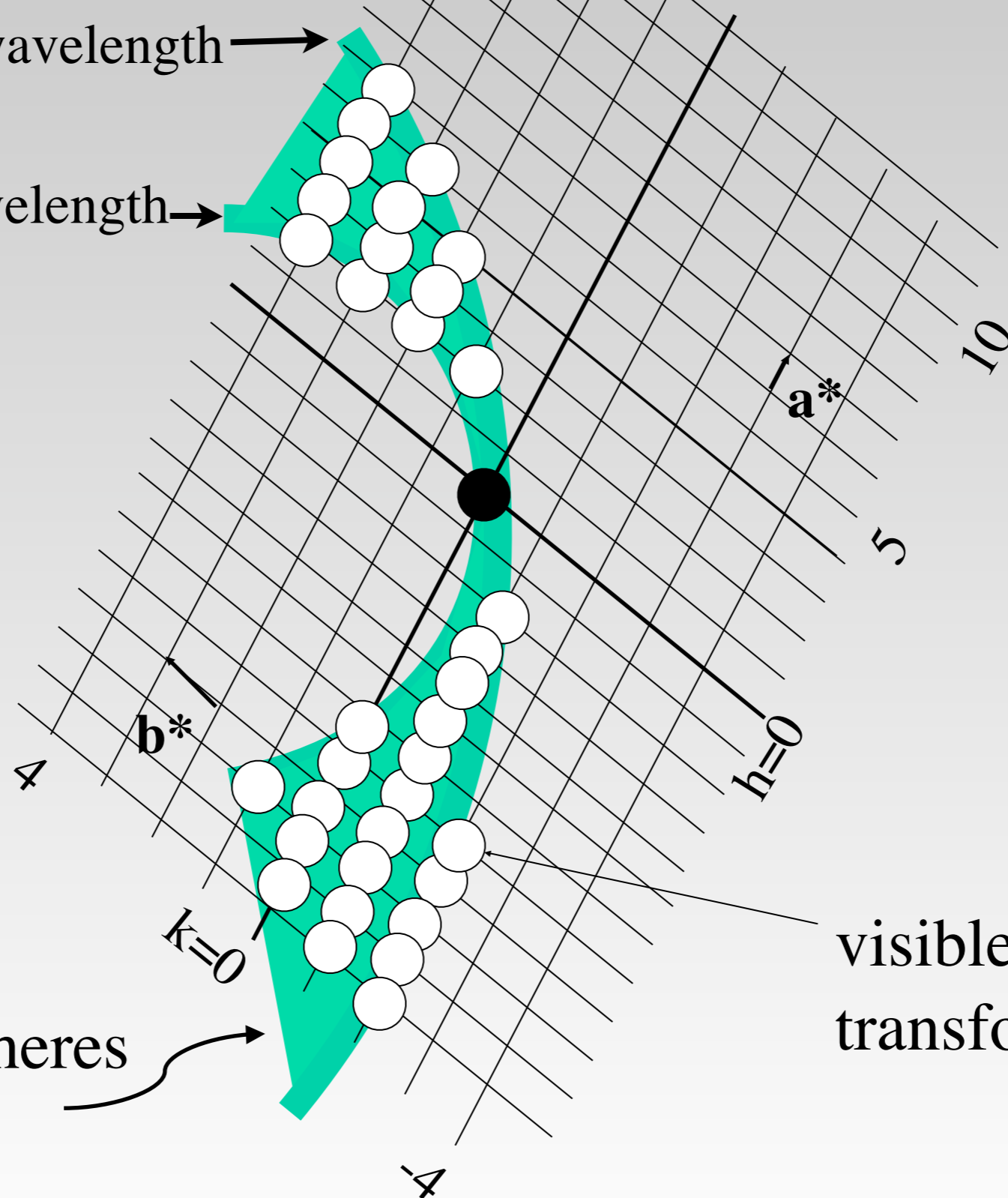
# Ewald sphere, monochromatic



# Ewald sphere, polychromatic

Reciprocal shortest wavelength →

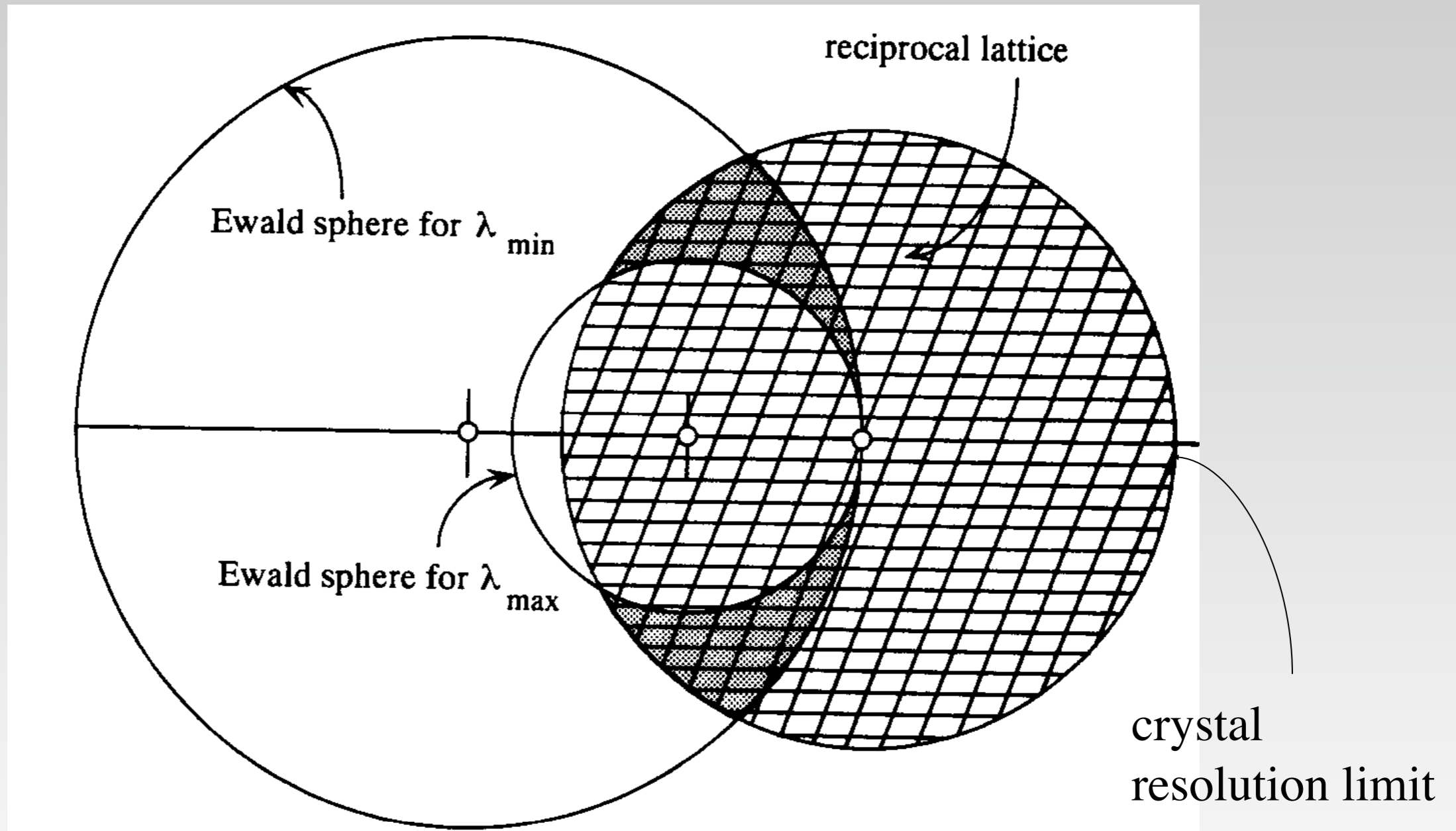
Reciprocal longest wavelength →



visible part of transform

Range of Ewald spheres

# The Ewald sphere(s), polychromatic



Ewald sphere has radius  $1/\lambda$ . Longer wavelength X-rays cause the Ewald sphere to shrink, picking up a different part of the reciprocal lattice.



# Cruikshank's dilemma

Bragg's Law for one wavelength

$$n\lambda = 2d \sin \theta$$

Bragg's Law for multiple wavelengths

$$\begin{aligned} n\lambda_{\max} &= 2d \sin \theta \\ &= n\lambda_{\max} / 2 = 2(d/2) \sin \theta \\ &= n\lambda_{\max} / 3 = 2(d/3) \sin \theta \end{aligned}$$

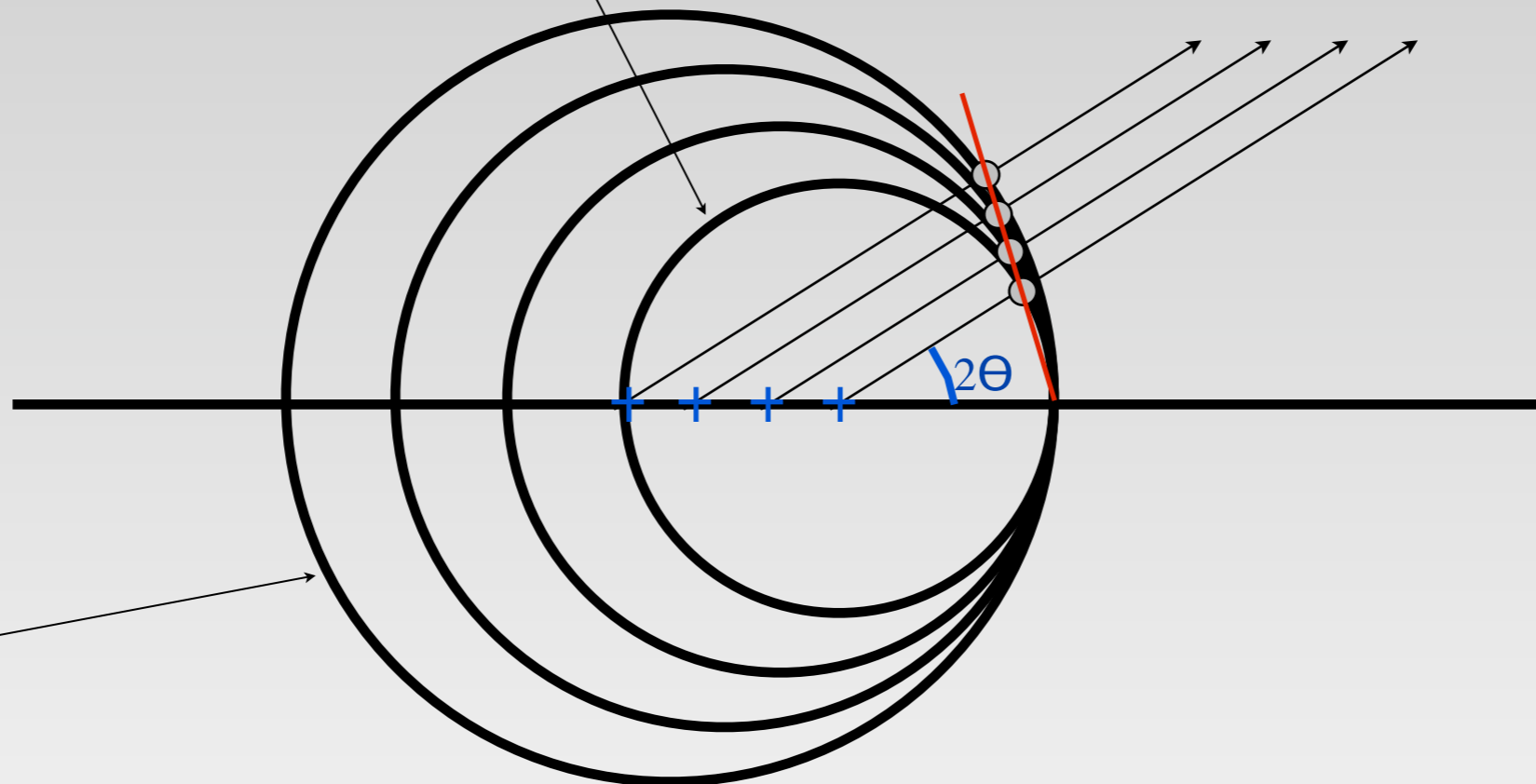
**In monochromatic crystallography, one  $\theta$  angle translates to one  $d$  (one resolution). In Laue crystallography, one  $\theta$  angle translates a range of  $d$ . How do we know which wavelength produced the reflection??**

# harmonic reflections

Ewald sphere for  $\lambda_{\max}$

harmonic F's all fall on the same spot on the film.

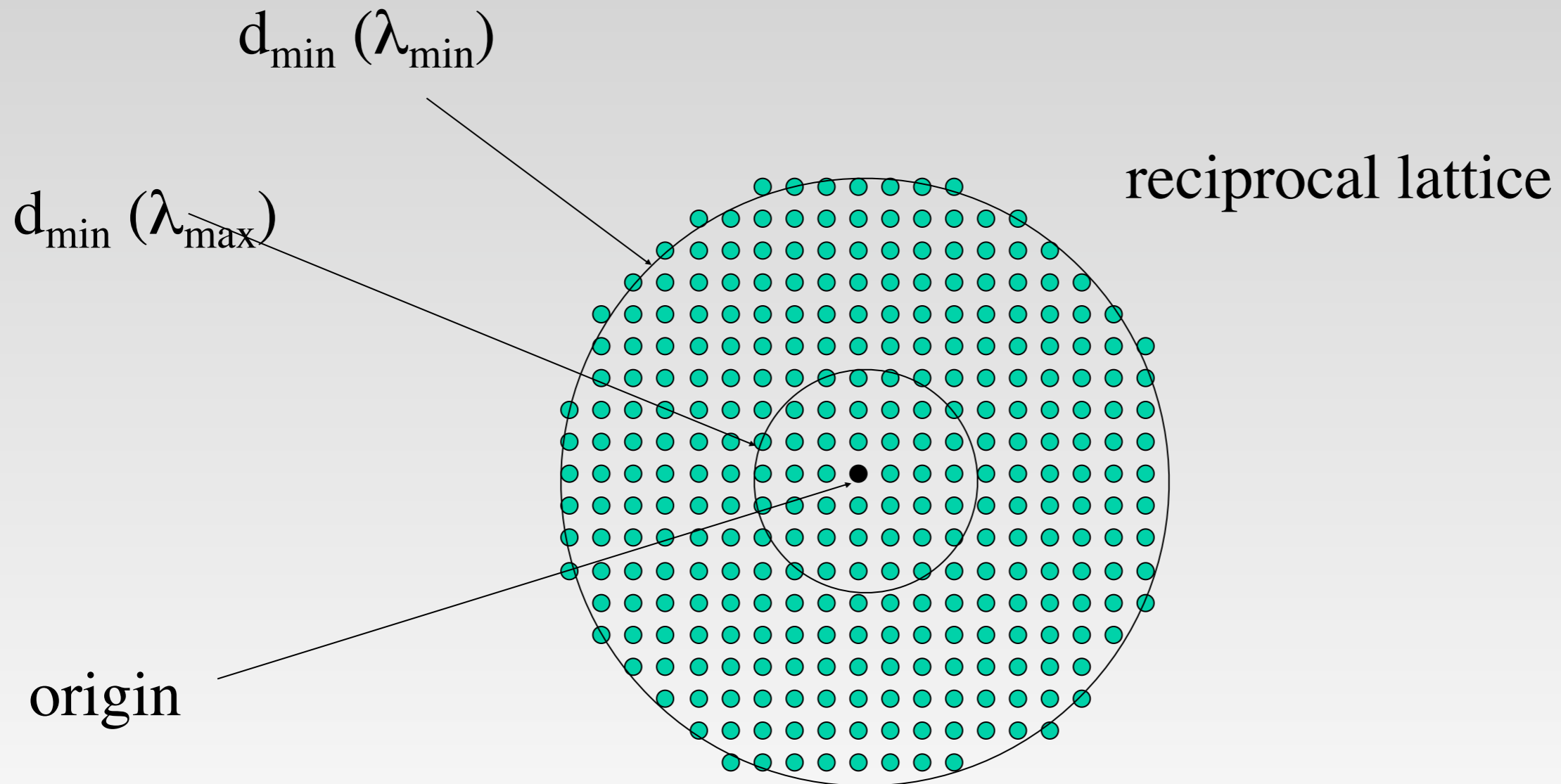
Ewald sphere for  $\lambda_{\min}$



Harmonic reflections  $(nh, nk, nl)$  have the same  $S$  direction, but the length is inversely proportional to  $\lambda$ . So  $(h, k, l)$  at  $\lambda = 2.0 \text{ \AA}$  and  $(2h, 2k, 2l)$  at  $\lambda = 1.0 \text{ \AA}$  diffract to exactly the same spot on the film.

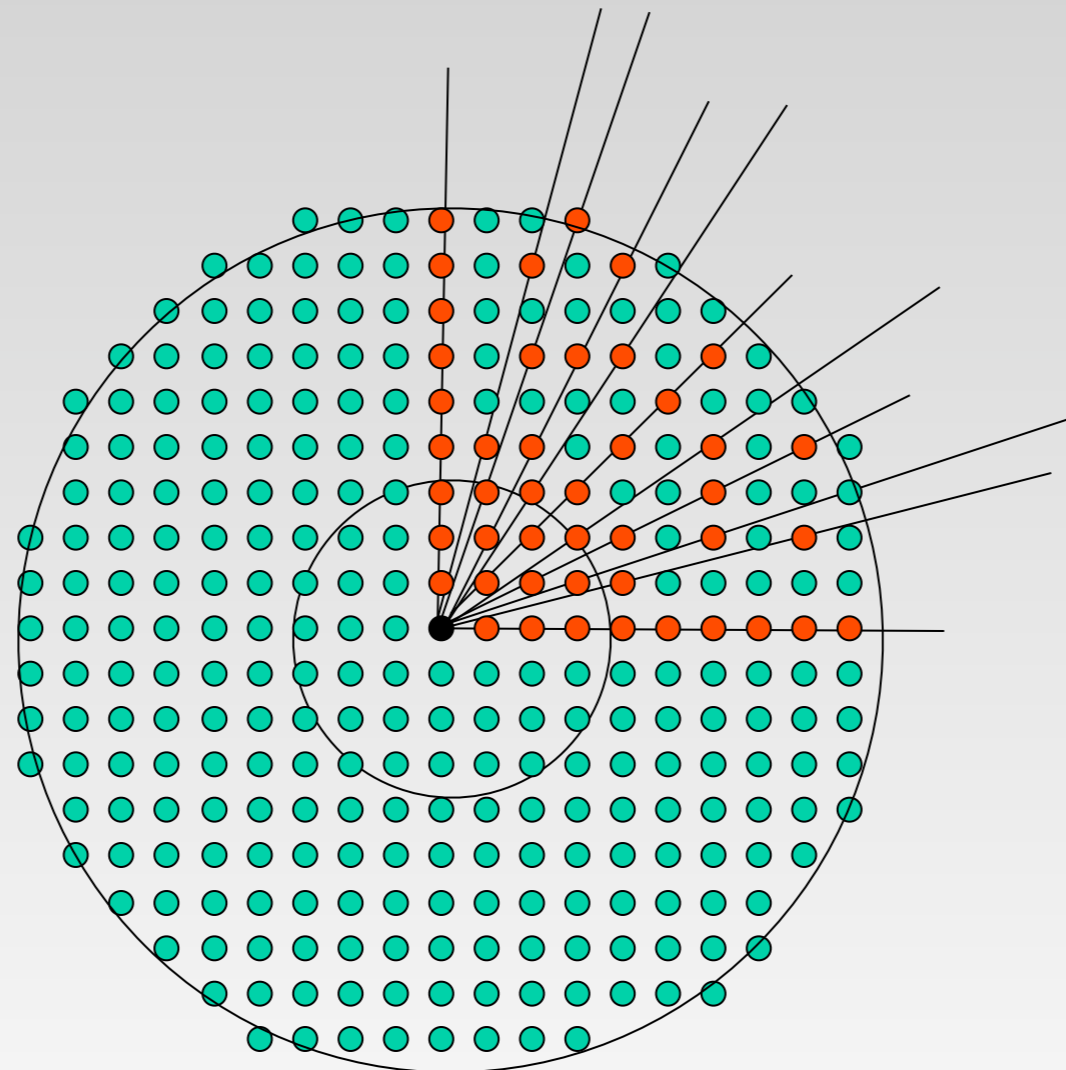
# Which reflections are multiples?

## Analogy to trees in an orchard



Summing harmonics is like viewing a lattice from the origin.  
Every line of sight represents one spot on the film.

# Which reflections are multiples? Analogy to trees in an orchard

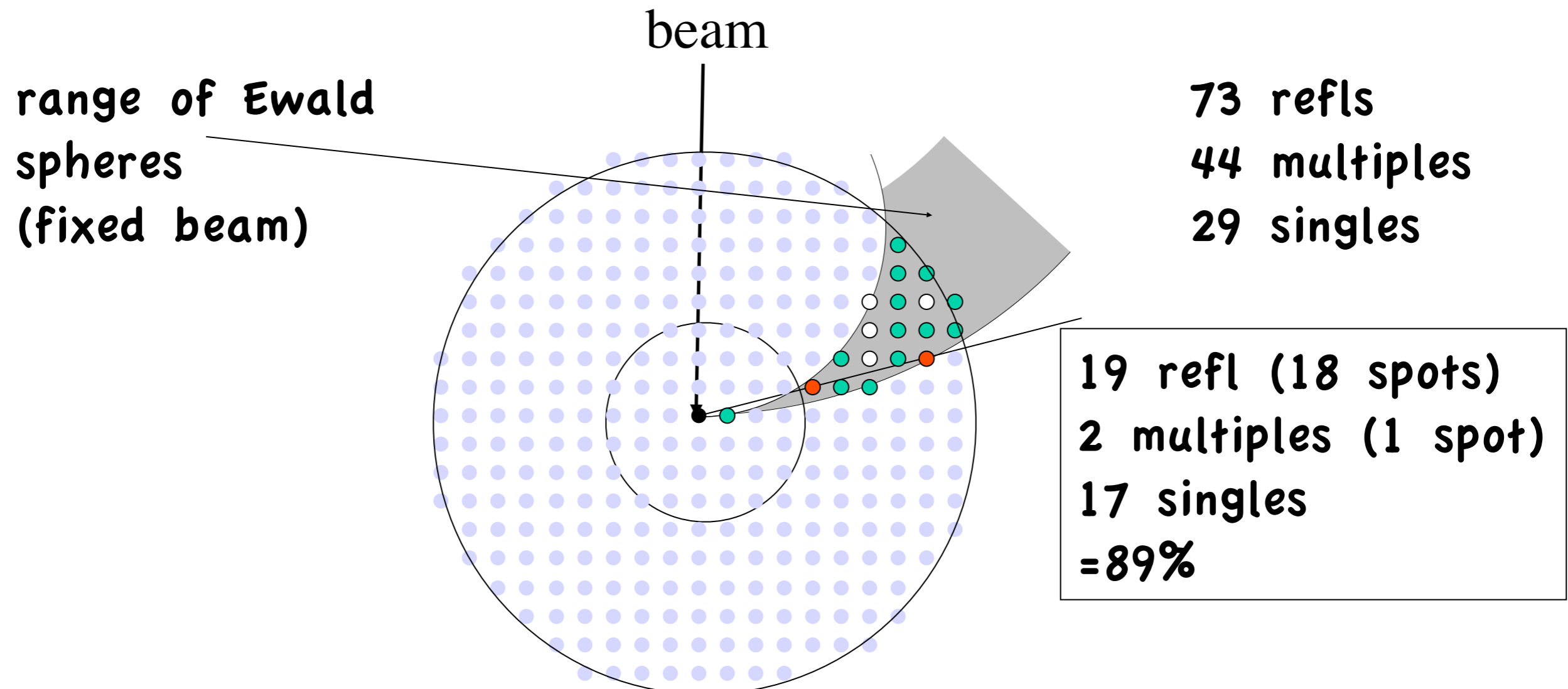


73 refls  
44 multiples  
29 singles

Standing in the middle of a circular orchard, how many tree trunks you see are hiding other tree trunks (“multiples”, red)? And how many are not (“singles”, green)?

# Which reflections are multiples?

## Analogy to trees in an orchard



Now cut down all the trees except the ones that are on the Ewald sphere for one of the wavelengths (range  $\lambda_{\min}-\lambda_{\max}$ ). Only the trees in the grey region remain. How many are multiples?

# Solving for missing intensities (after the fact)

$n=1,2,3$  etc. within  
“Cruickshank range”

$$I(nh, nk, nl) = \sum_n \frac{|F(nh, nk, nl)|^2}{f(\lambda(F))}$$

total intensity for all  
harmonics in range

Scale factors. A  
function of  
wavelength,  
polarization, etc.

Unknown amplitudes

Scale factors ( $f$ ) may be found for singles.

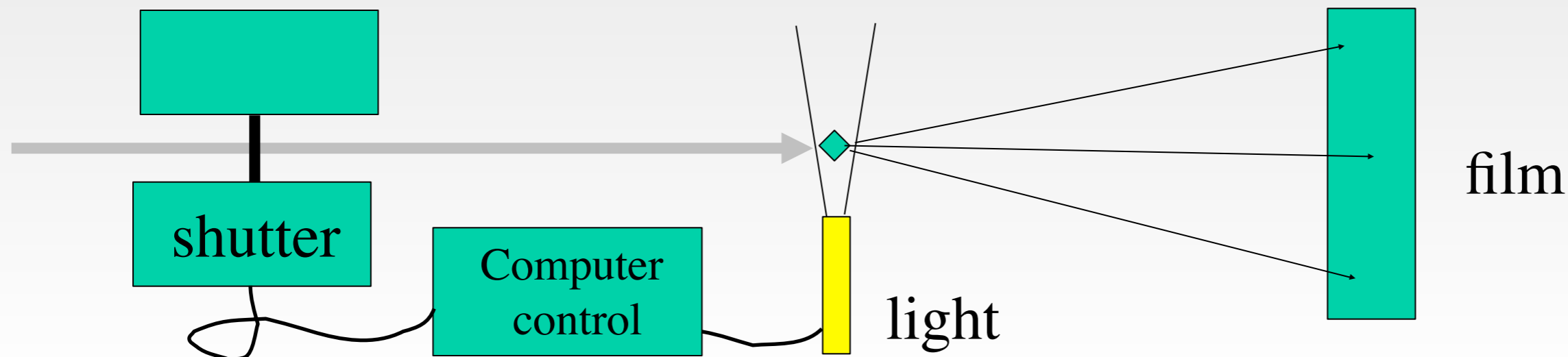
Then, each multiple is a linear equation of the unknown  $F^2$ 's,  
which can be solved during *least squares refinement*.

# Time-resolved crystallography

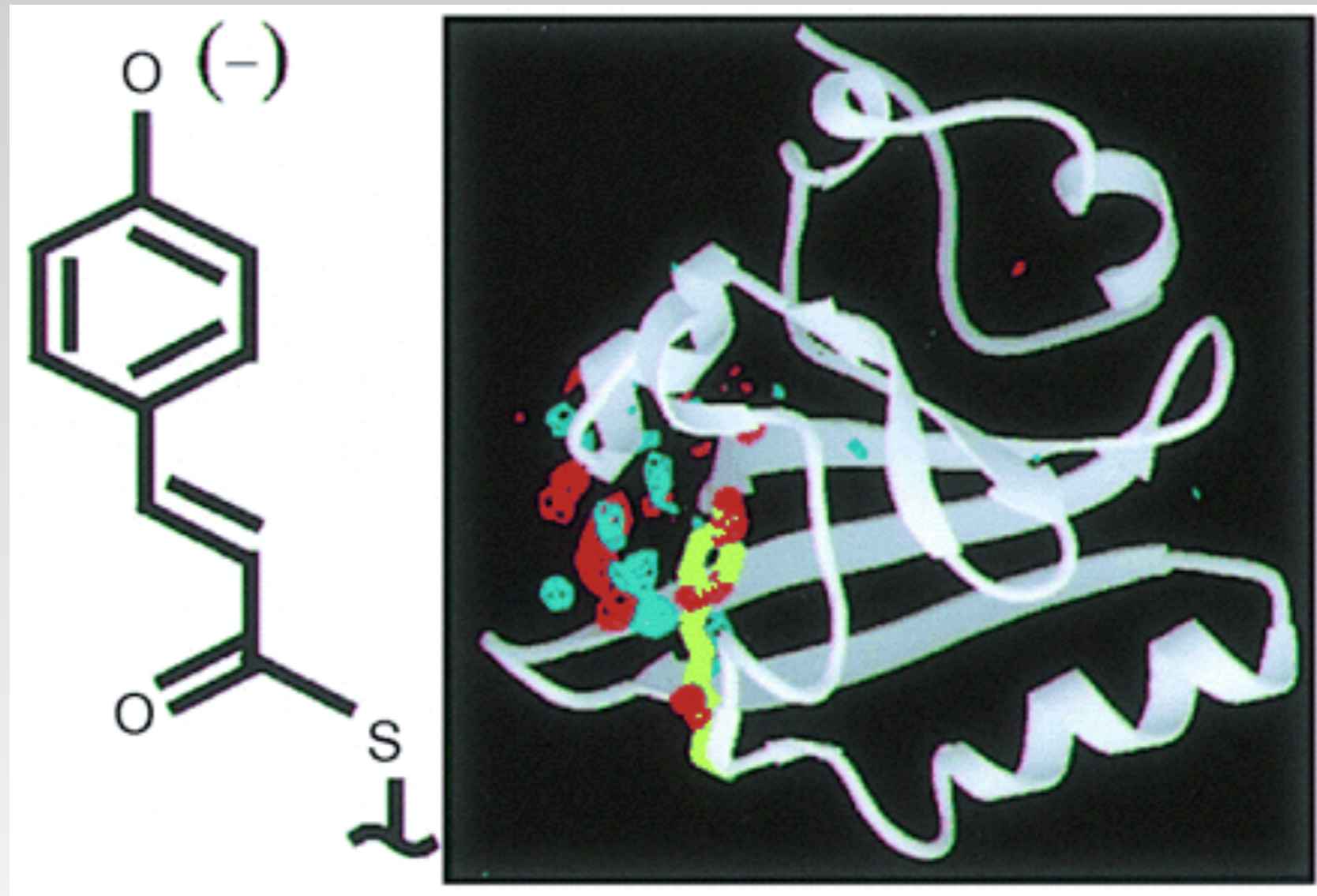
If a reaction can be initiated in a crystal, simultaneously throughout the crystal, then Laue photography can capture the structural changes at the ns ( $10^{-9}$  s) to ms ( $10^{-3}$  s) timescale.

Crystals must withstand ultrahigh fluxes of X-rays, or are destroyed in the process.

Light-initiated reactions can be studied using the Laue method.



# Photoactive yellow protein



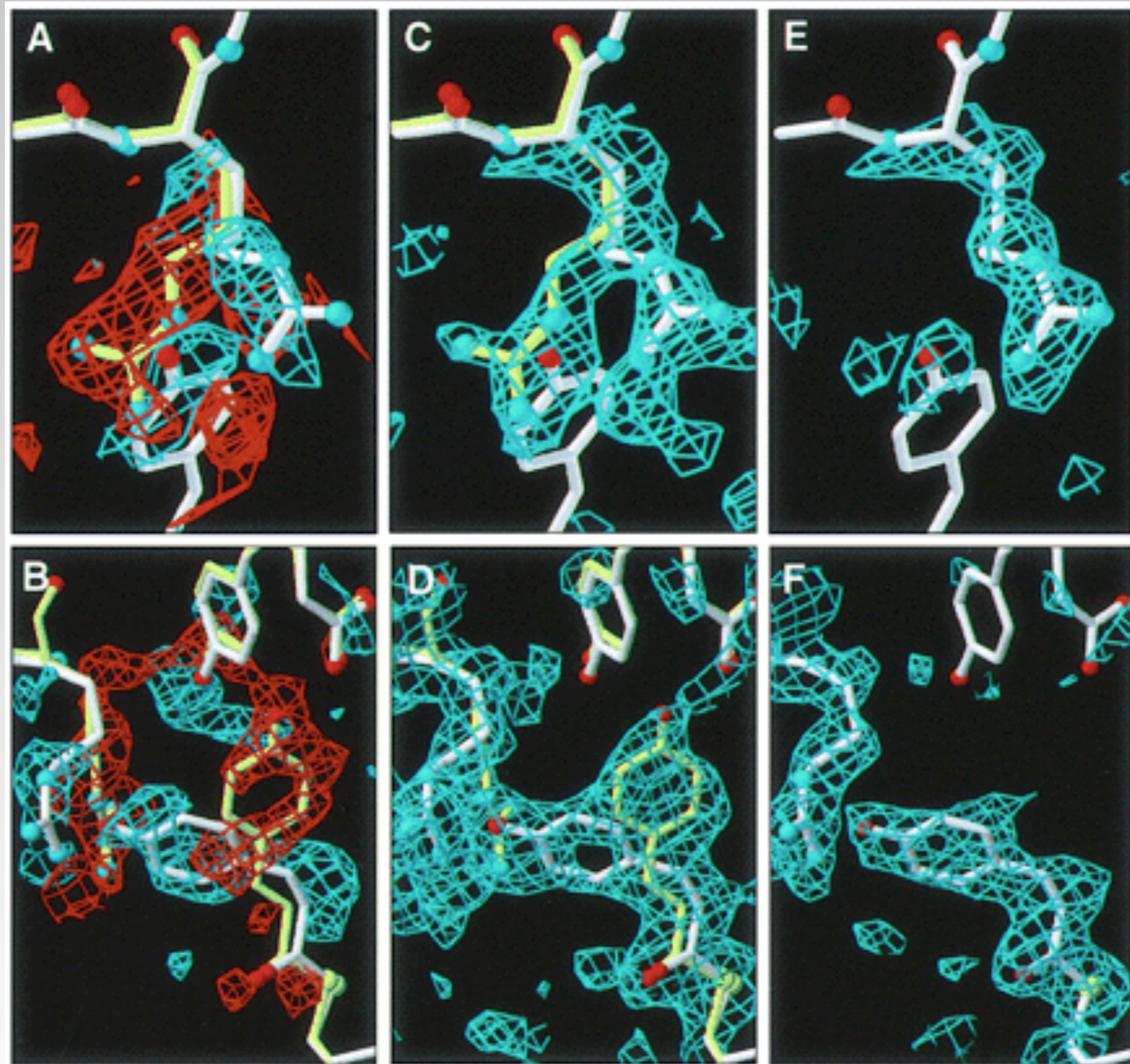
4-hydroxycinnamyl  
chromophore

Photoactive yellow protein (from the  
phototrophic bacterium *Ectothiorhodospira*  
*halophila*)



# Hybrid maps

$$F_{\text{bleached}} - F_{\text{dark}}$$



difference  
density

omit  
map

extrapolated  
density

# Advantages of Laue method

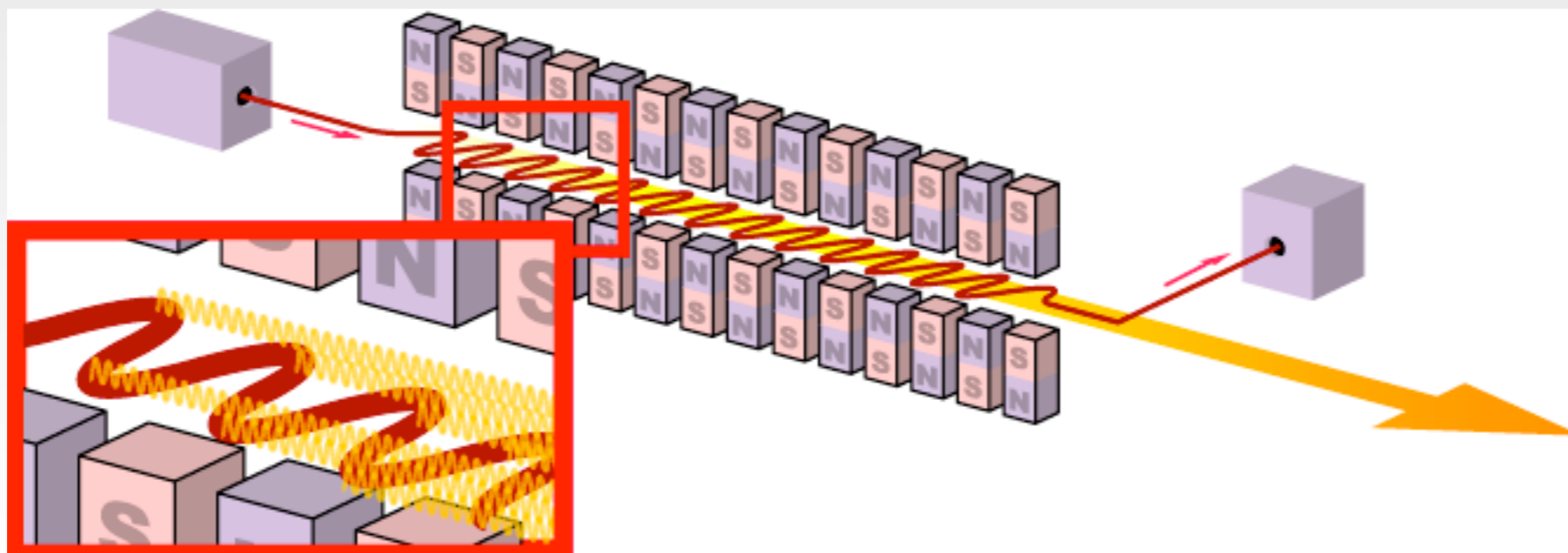
- **Extremely short data collection time.**
- **Time-resolved.**
- **Just a few exposures covers reciprocal space, especially for high-symmetry space groups.**

# Problems with Laue method

- Unbalanced coverage of reciprocal space.
- Crystals must withstand intense short exposures, or many crystals must be used.
- Time-resolved study usually means crystals cannot be frozen, making them vulnerable to X-ray damage.
- Spacial overlap requires low mosaicity, small beam, crystal.

# X-ray free electron laser (XFEL)

- First successful X-ray laser, published in July 2012.
- Generated by an electron beam which moves freely through a magnetic structure, under vacuum.
- Tunable to a wide range of frequencies.
- Billions of times more intense than conventional methods.

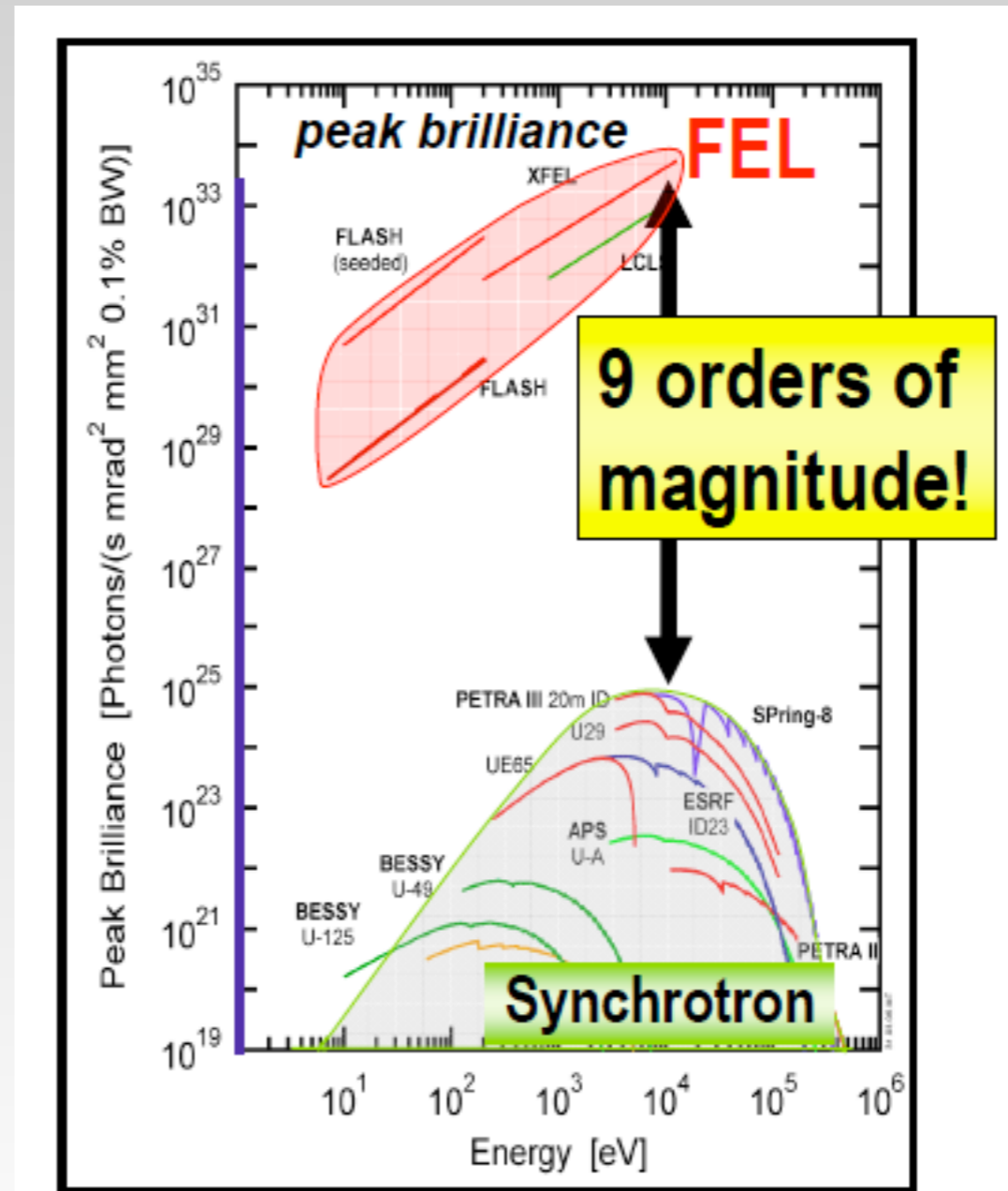


# European FEL construction site, Hamburg



# Free electron laser

- $10^{12-13}$  photons:  $\sim 10$  fs pulses
- repetition rate: now 120 Hz
- photon energies: 10 keV
- transversally: fully coherent



Images borrowed from Thomas Barends  
google: Barends FEL Nanocrystallography

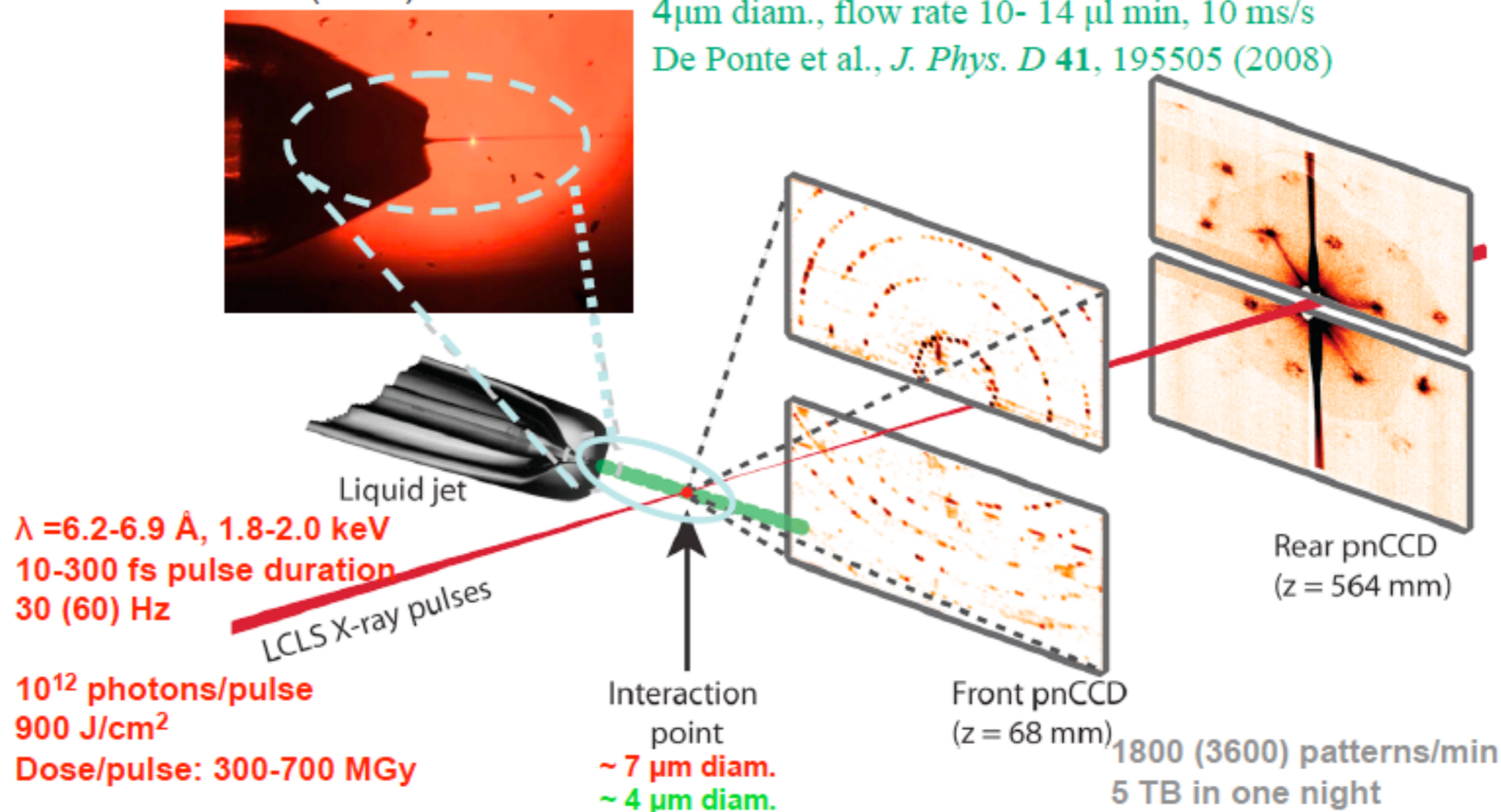
# First serial femtosecond crystallography experiments at LCLS/AMO/CAMP

Chapman et al  
Nature 470: 73 (2011)

**Gas focussed liquid jet:**

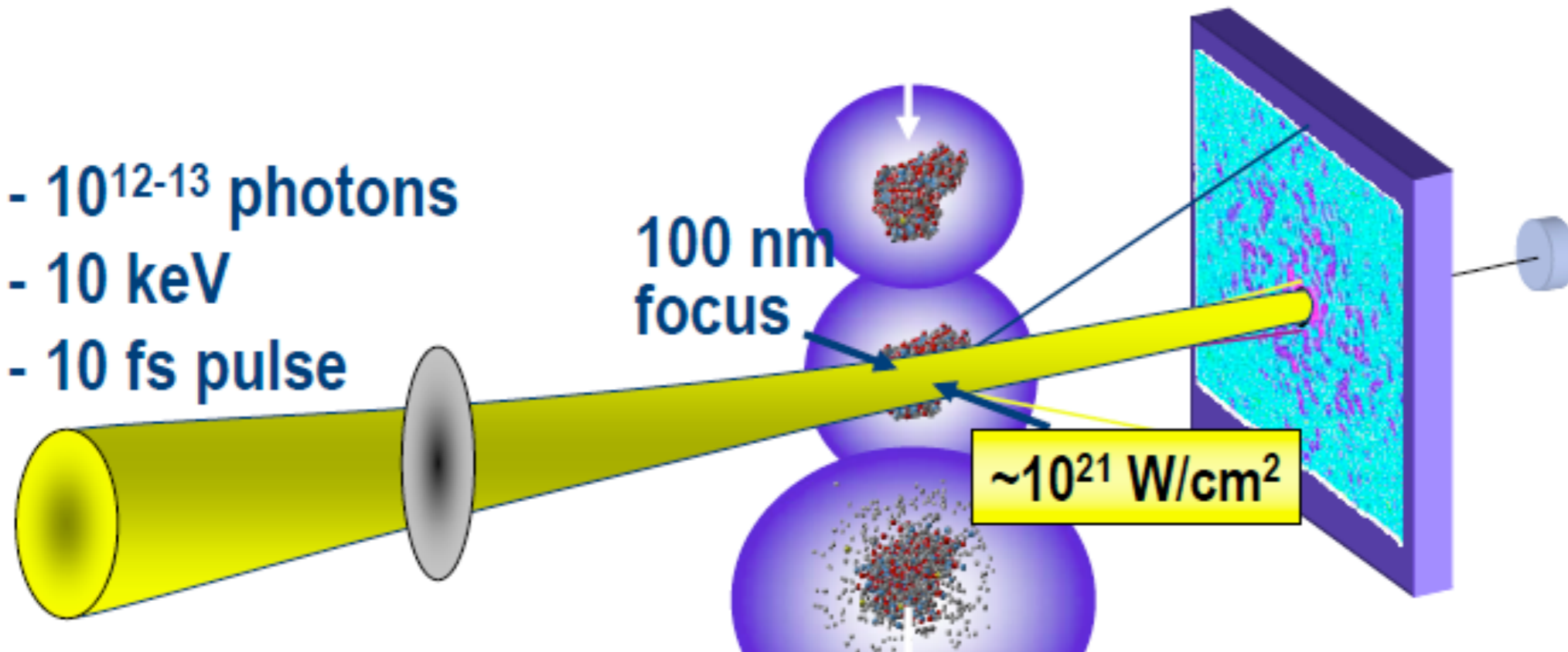
4 $\mu$ m diam., flow rate 10- 14  $\mu$ l min, 10 ms/s

De Ponte et al., *J. Phys. D* 41, 195505 (2008)



# Coherent Diffractive Imaging

- $10^{12-13}$  photons
- 10 keV
- 10 fs pulse



Calculations in vacuum, Neutze et al., Nature 2000



# So what's the *bad news*?

- Hit rates are low, + only a fraction of hits indexable
- → the method needs:
  - 1-to-several ml of highly concentrated (yoghurt-like!) suspension of microcrystals (hit rates are low, for high resolution many 10,000s images needed)

*How do you make that much protein?*

(usual yields are in the 0.1-1mg range for membrane proteins..., very difficult to produce, not stable!)

*Can you make nanocrystals of it?*

*(how do you know you have them?*

*how do you know they are any good?*

*testing them can only be done at the FEL...)*

*(can you inject them?*

*PEG/salts may clog the nozzle.....)*

*.....?*

DROPLET-ON-DEMAND  
TO SAVE SAMPLE ?  
HIGH PULSE RATE?

