

# **Molecular Modeling 2018**

Midterm review slides

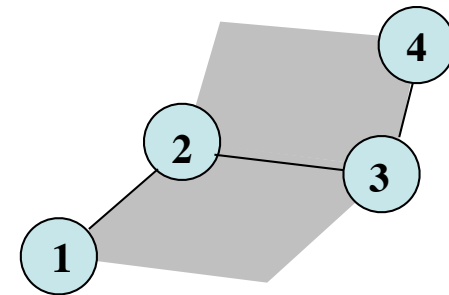
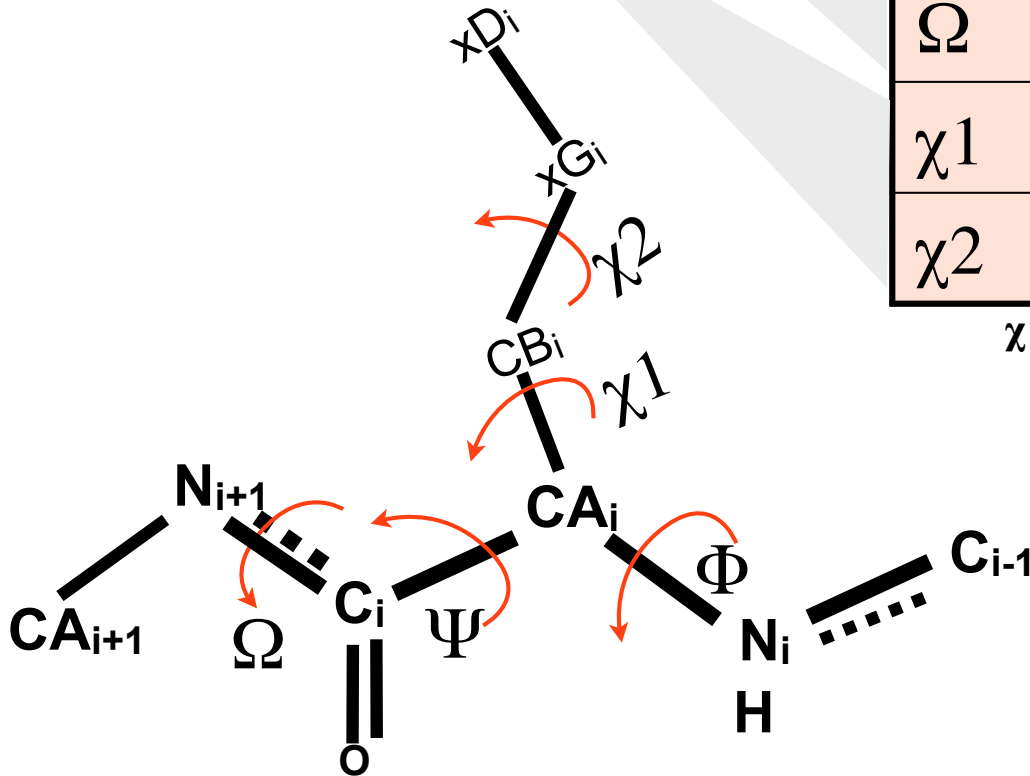
# Torsion angles

Protein flexibility is due to rotations around single bonds, backbone and side chain.

4 atoms define two planes

Angle	atom1	atom2	atom3	atom4
$\Phi$	$C_{i-1}$	$N_i$	$CA_i$	$C_i$
$\Psi$	$N_i$	$CA_i$	$C_i$	$N_{i+1}$
$\Omega$	$CA_i$	$C_i$	$N_{i+1}$	$CA_{i+1}$
$\chi_1$	$C_i$	$CA_i$	$CB_i$	$xG_i$
$\chi_2$	$CA_i$	$CB_i$	$xG_i$	$xD_i$

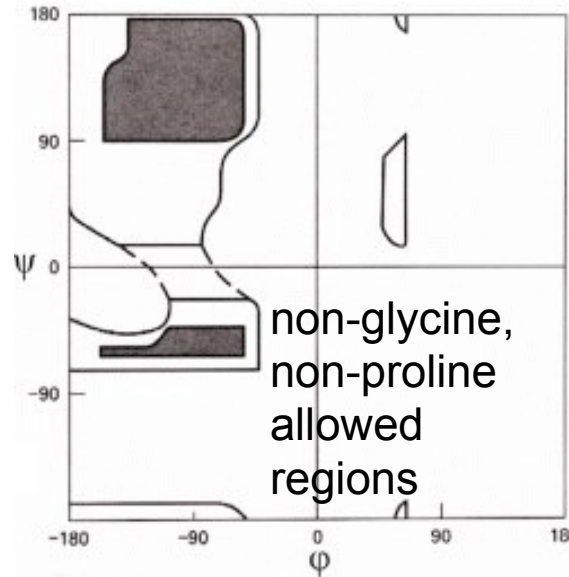
$\chi = \text{chi}$



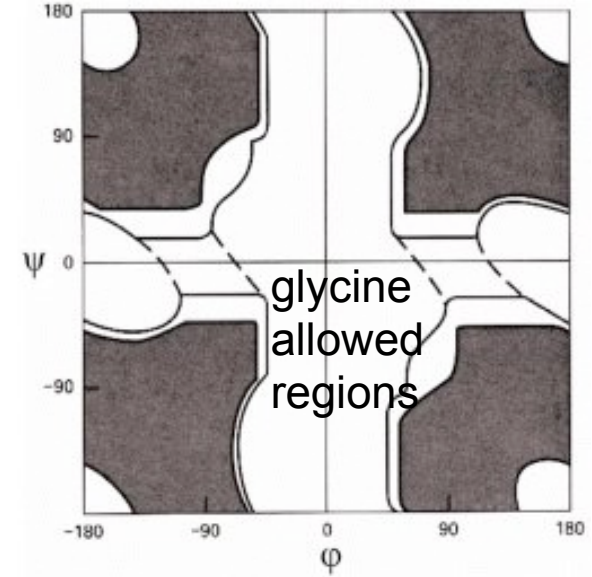
# Ramachandran Plot maps allowable phi, psi regions

Ramachandran used a physical model of dipeptides to determine the allowed (dark) and disallowed (white) combinations of phi and psi backbone angles. The observed frequencies roughly agree with R's allowed regions.

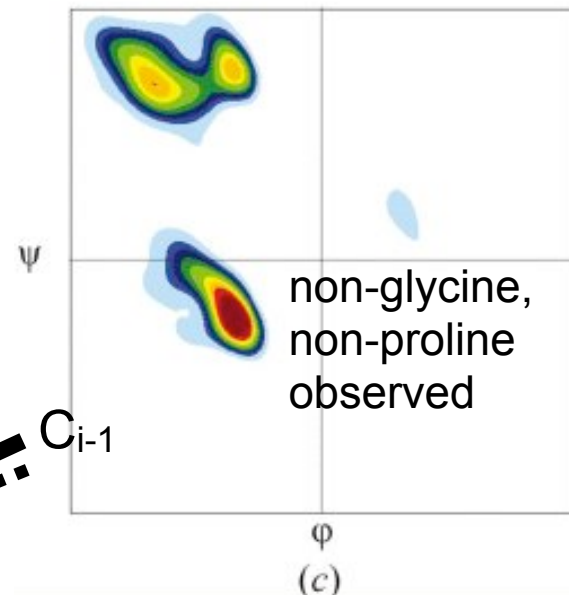
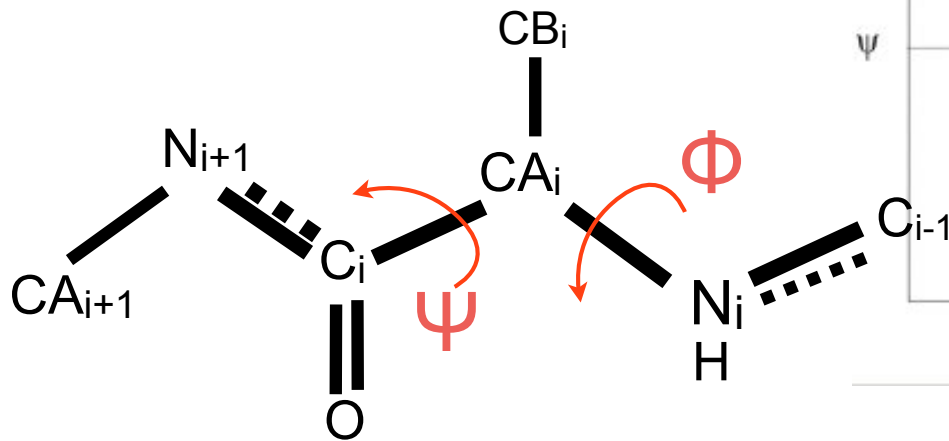
Ramachandran & Sasisekharan (1968)



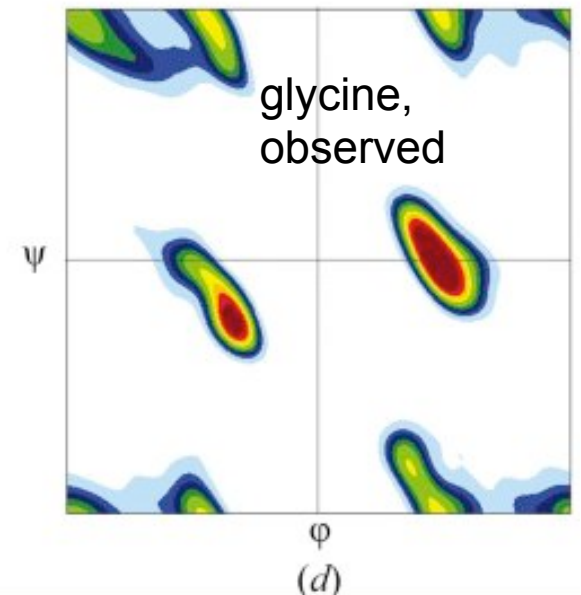
(a)



(b)



(c)



(d)

# Structure quality: resolution

- Resolution =  $d$  in Bragg's Law.  $n\lambda=2d \sin\theta$ . Lower  $d$  is higher resolution.
- “Resolution” = resolution limit = the lowest  $d$  observed = the highest scattering angle observed.

Resolution	quality
> 4Å	nearly worthless, shows blobs of density
3-4Å	medium. Shows backbone and some sidechains.
2-3Å	typical good structure, all sidechains visible
1.5-2Å	high resolution. Atom positions known within 0.1Å rmsd.
< 1.5Å	ultra high resolution! Hydrogens sometimes visible.

# SCOP fold jargon

example:  $\alpha/\beta$  proteins: flavodoxin-like

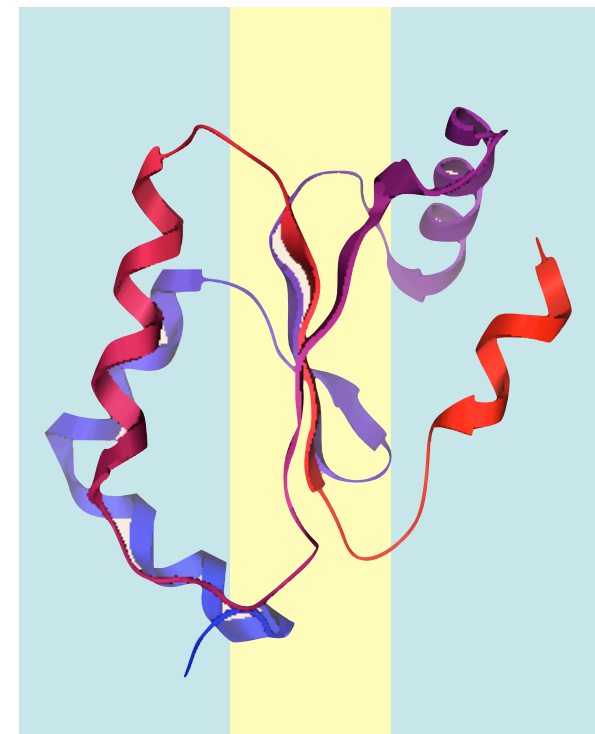
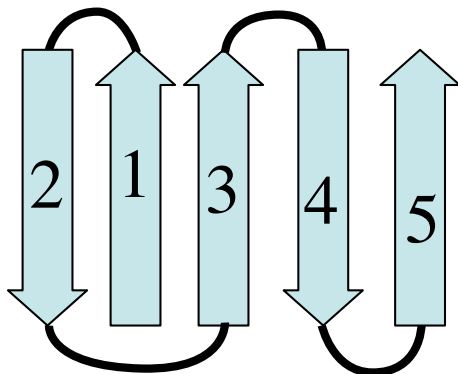
SCOP Description: 3 layers,  $\alpha/\beta/\alpha$ ; parallel beta-sheet of 5 strand, order 21345

Note the term: “*layers*”

Rough arrangements of secondary structure elements.

Note the term: “*order*”

The sequential order of beta strands in a beta sheet.



$\alpha$  layer

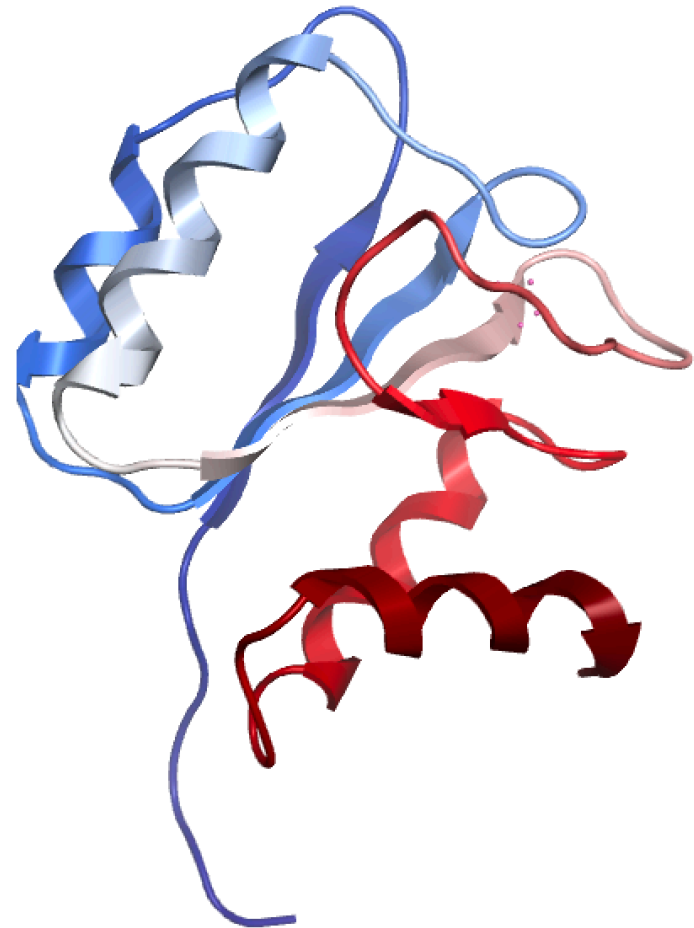
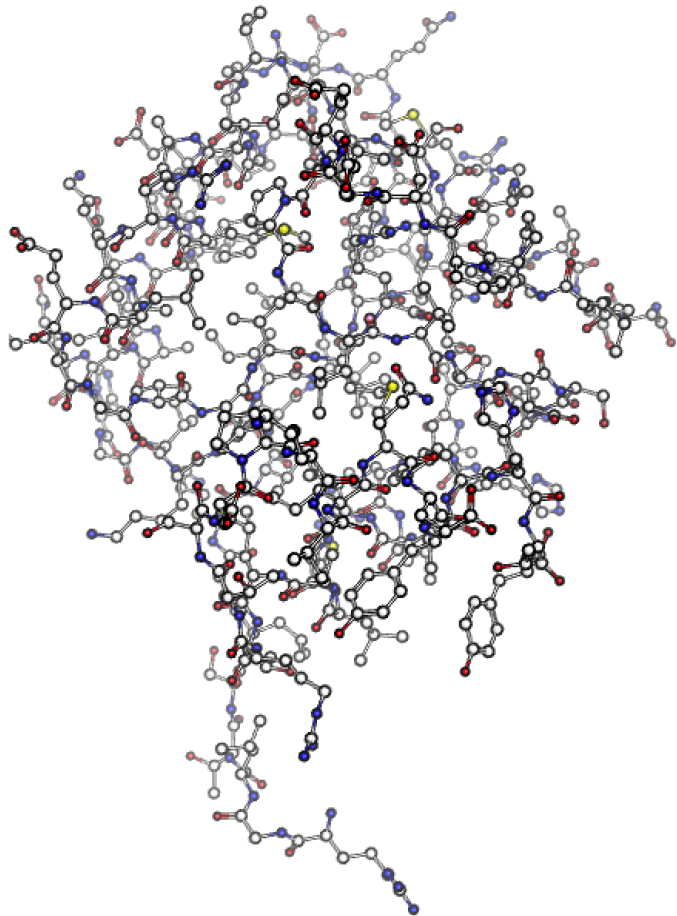
$\alpha$  layer

$\beta$  layer

# How to draw TOPS

On course website, find the link "**TOPS practice**" ([tops\\_practice.moe](#))

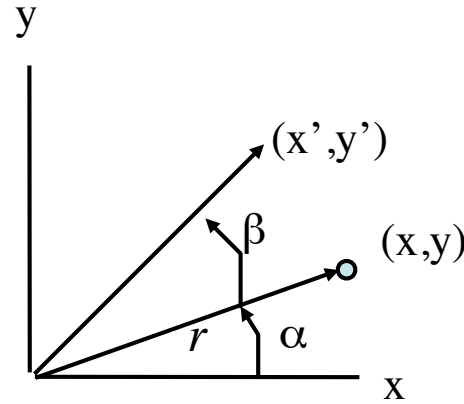
Save it. Open it in moe.



## A rotation matrix

$$x = r \cos \alpha$$

$$y = r \sin \alpha$$



$$x' = r \cos (\alpha + \beta)$$

$$= r (\cos \alpha \cos \beta - \sin \alpha \sin \beta)$$

$$= (r \cos \alpha) \cos \beta - (r \sin \alpha) \sin \beta$$

$$= x \cos \beta - y \sin \beta$$

$$y' = r \sin (\alpha + \beta)$$

$$= r (\sin \alpha \cos \beta + \sin \beta \cos \alpha)$$

$$= (r \sin \alpha) \cos \beta + (r \cos \alpha) \sin \beta$$

$$= y \cos \beta + x \sin \beta$$

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} r \cos \alpha \\ r \sin \alpha \end{pmatrix} = \begin{pmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

rotation matrix is the same for any  $r$ , any  $\alpha$ .

# RMSD

Root Mean Square Deviation in superimposed coordinates is the standard measure of **structural difference**.

$$\sqrt{\frac{\sum_{i=1,N} (\vec{v}^1_i - \vec{v}^2_i)^2}{N}}$$

Where  $\vec{v}^1_i$  and  $\vec{v}^2_i$  are the *equivalent\** *coordinates* from molecules 1 and 2, respectively.

\*Equivalent as defined by an **alignment**.



# Chicken/Egg

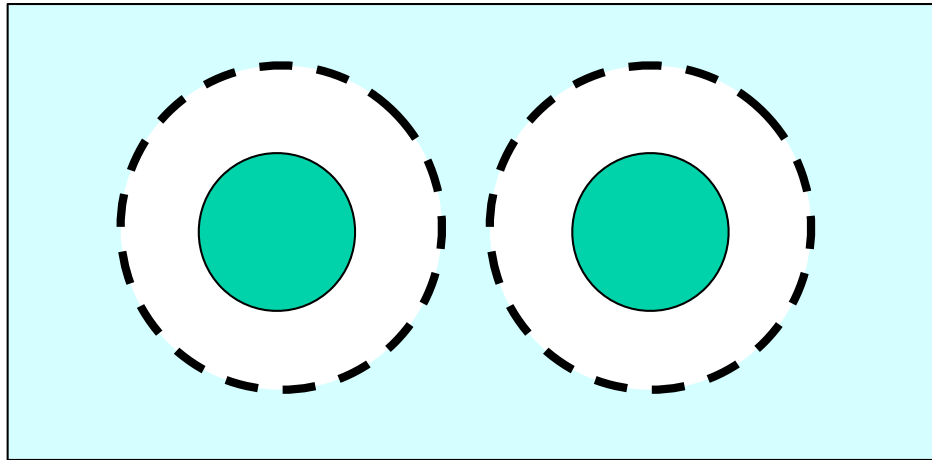
- Least squares superposition defines the alignment.
- The alignment defines the least squares superposition.

# What is energy?

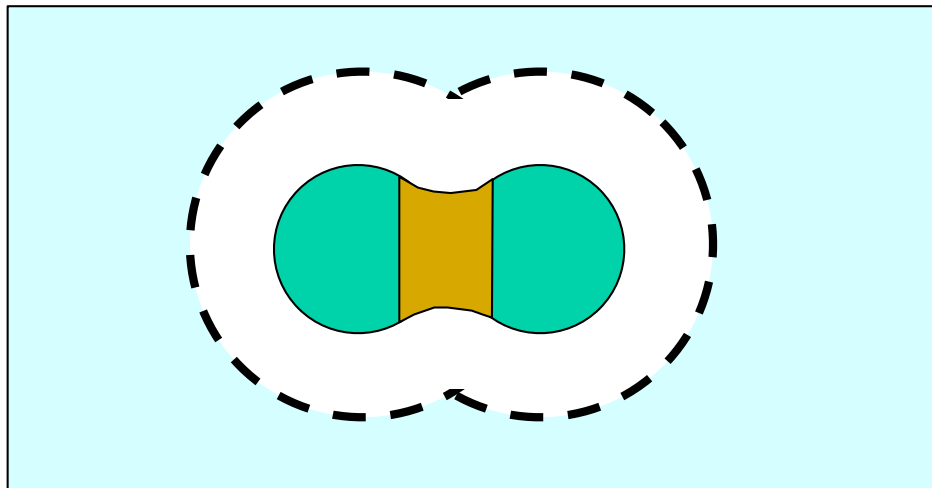
- **Energy (G)** is a measure of the **probability** of the **state of the system**. Energy is the **negative log of the probability ratio, times temperature**.
- $\Delta G = -RT \ln ( A / \text{not } A )$   
or  $-RT \ln( P / (1-P) )$ , where  $P = \text{probability}$ .
- The system = the atoms.
- State = where the atoms are.  
(This is a vague definition so we can be flexible about what the energy means.)
- Energy is always relative.
- Energy is measured between two states.
- Energy is expressed in J/mole, or kJ/mole.
- Energy breaks down into enthalpy (H) and entropy (S).  
 $\Delta G = \Delta H - T\Delta S$ .
- Energy also breaks down to **potential** energy and **kinetic** energy.

# The Hydrophobic Effect

Solvent accessible surface (dashed line) around non-polar atoms contains "high energy waters" because those waters lose H-bonds.



Non-polar atoms come together because it decreases the number of high energy waters. (Even at the cost of creating void space (brown)).

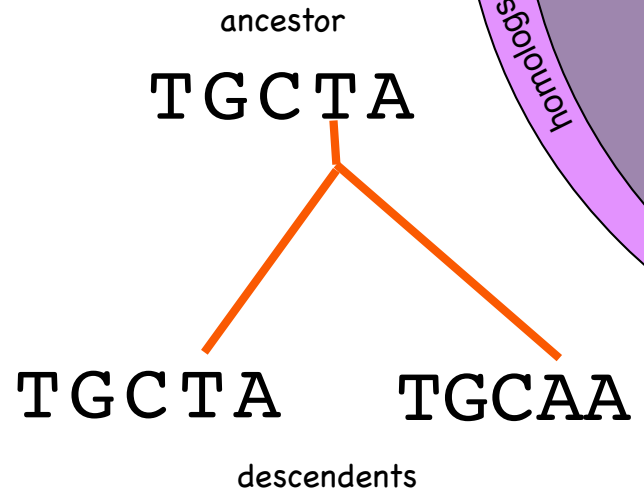
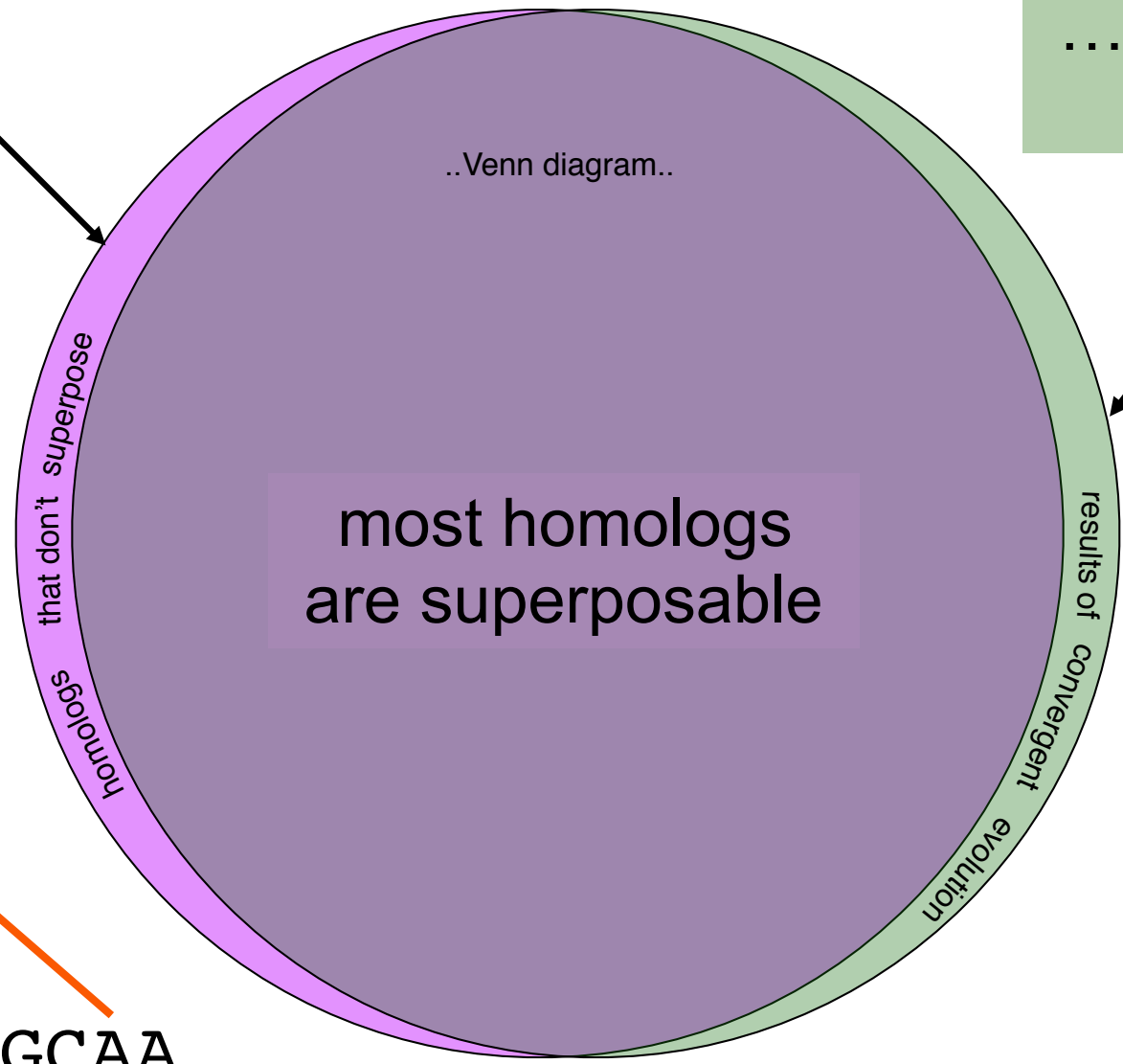


# The rule: similar sequence means similar structure

sequences that...

...have a common ancestor

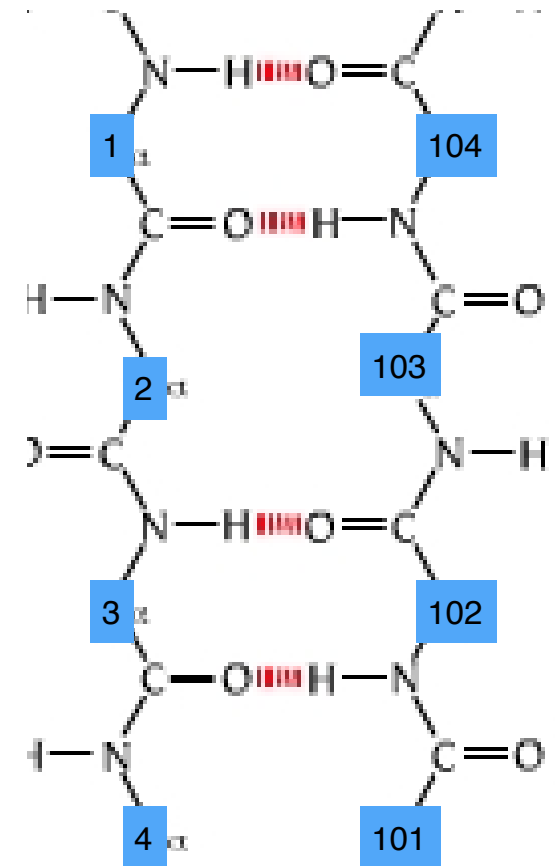
...superimpose in space



# Secondary structure using matrices: antiparallel sheet

0	1	0
1	0	0

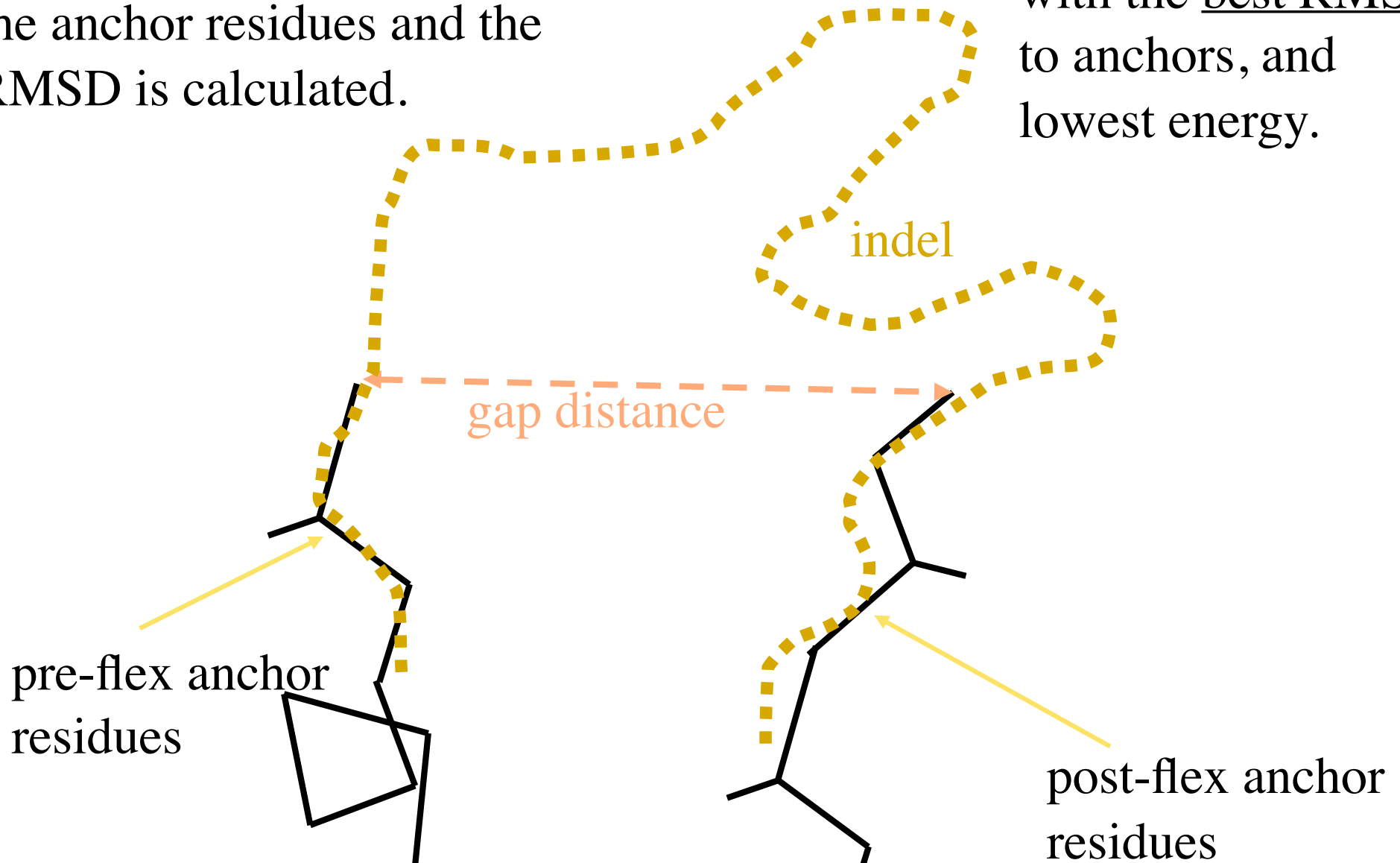
0	1	-2
1	0	+2



# Automated Loop Search

Loops of the right length in the database are superimposed on the anchor residues and the RMSD is calculated.

MOE keeps the loops with the best RMSDs to anchors, and lowest energy.



# Telling MOE how to anchor a better loop search

target	ACDEF	G . . . . . H	IKLMNP .	QRSTVWY
	:	:	:	
template	. CDDE	. GACDGH .	IYIM . . Q . Q	STVWF

Align F to F, I to I, delete GACDGH and add 2-residue loop GH from a loop search.

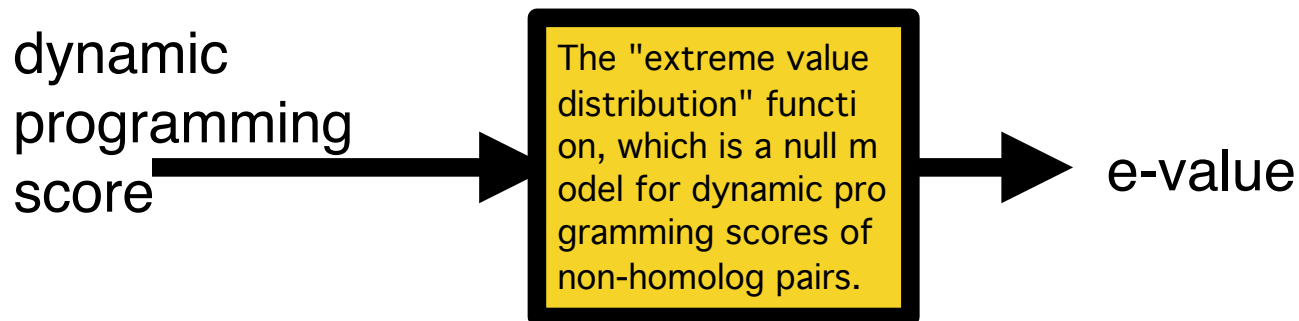
2-for-6  
instead of 0 for 4.

Align M to M, R to Q<sub>(2)</sub>, delete Q and add a 3-residue loop NPQ from a loop search.

3-for-1  
instead of 2 for 0.

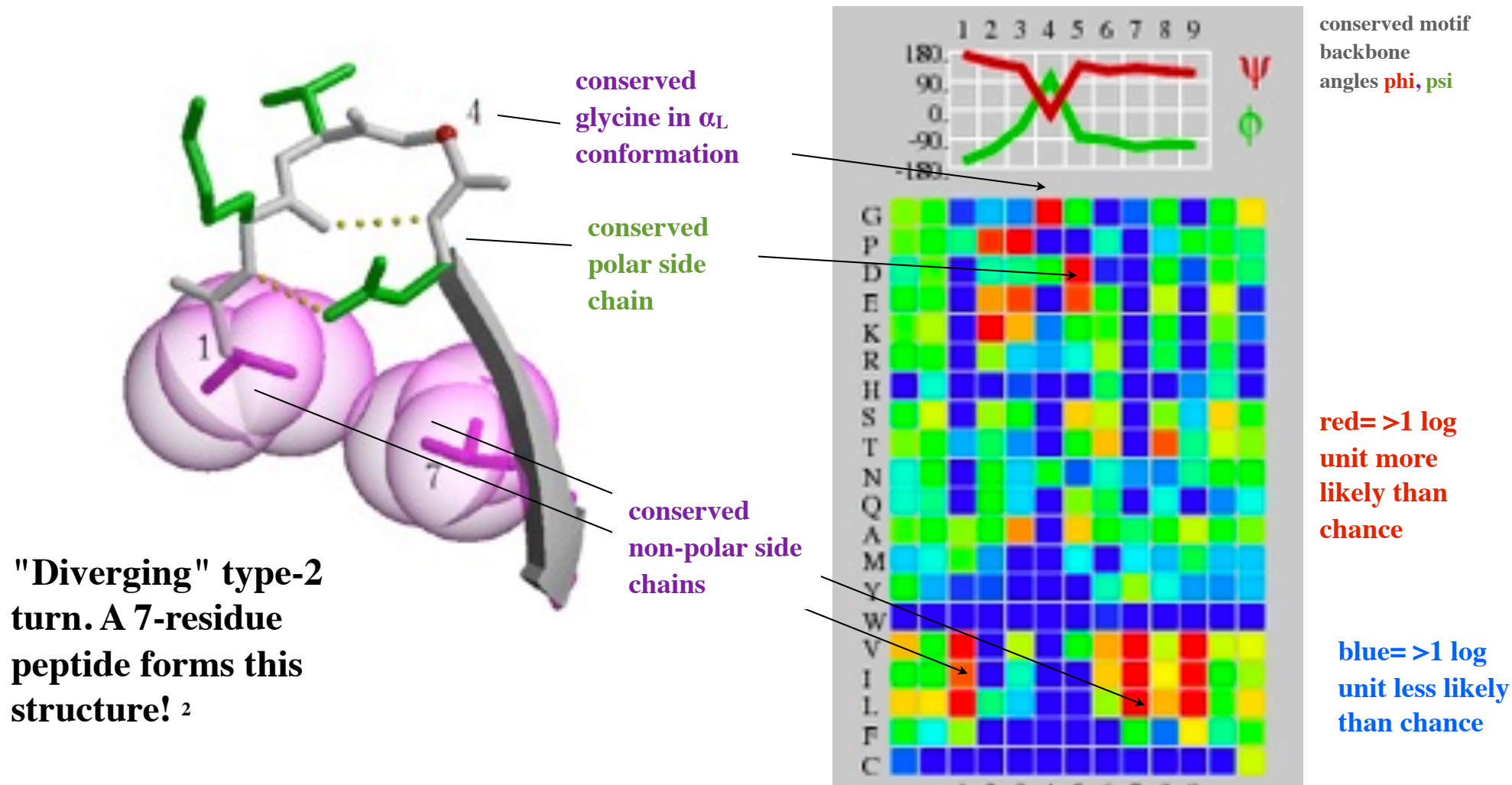
# e-value

- The number of times in a database search that you will get a random, non-homologous hit with the same score or better.





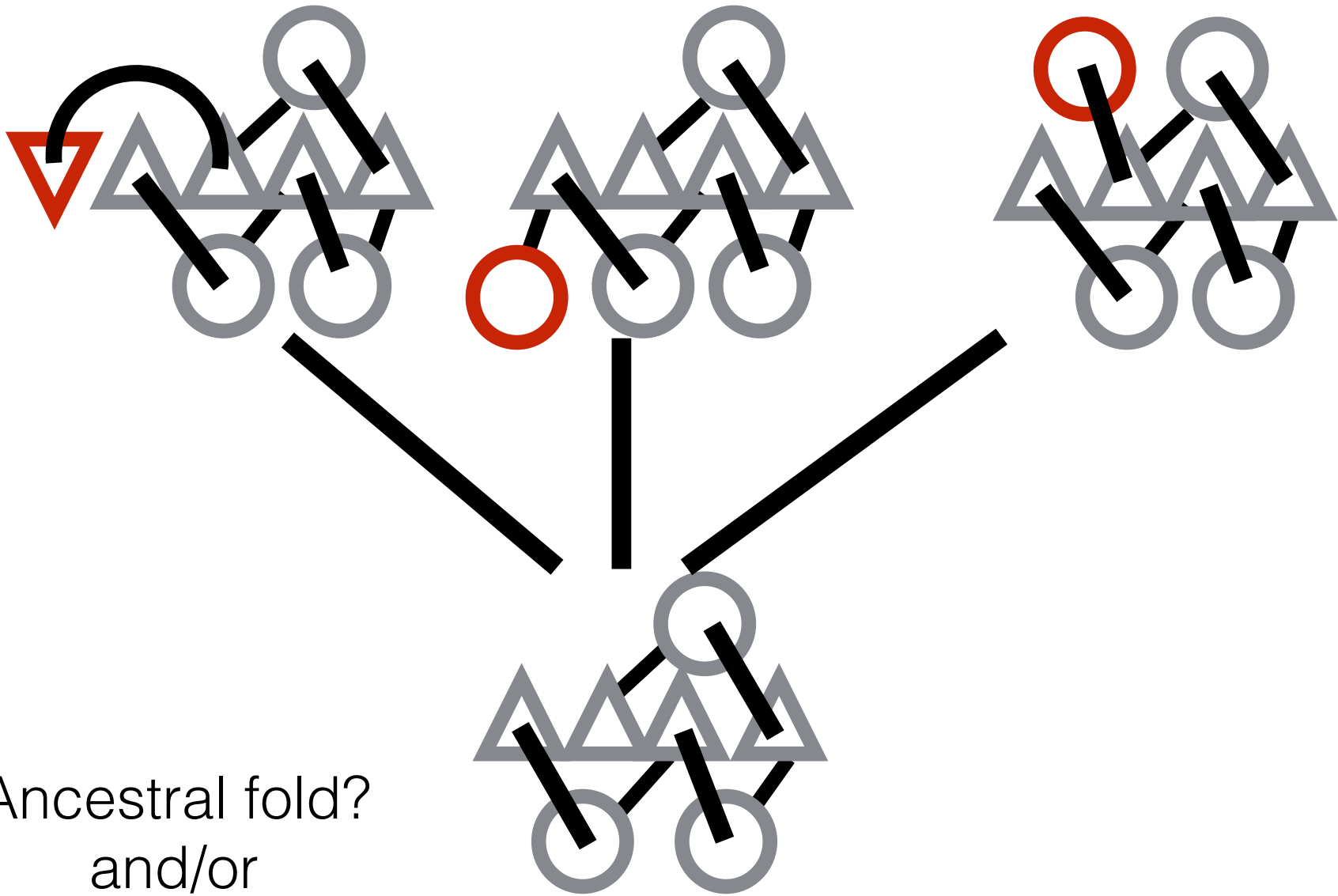
# Biophysics of an I-sites motif



<sup>1</sup>Bystroff C & Baker D. (1998). Prediction of local structure in proteins using a library of sequence-structure motifs. *J Mol Biol* 281, 565-77.

<sup>2</sup>Yi Q, Bystroff C, Rajagopal P, Kleivit RE & Baker D. (1998). Prediction and structural characterization of an independently folding substructure in the src SH3 domain. *J Mol Biol* 283, 293-300.

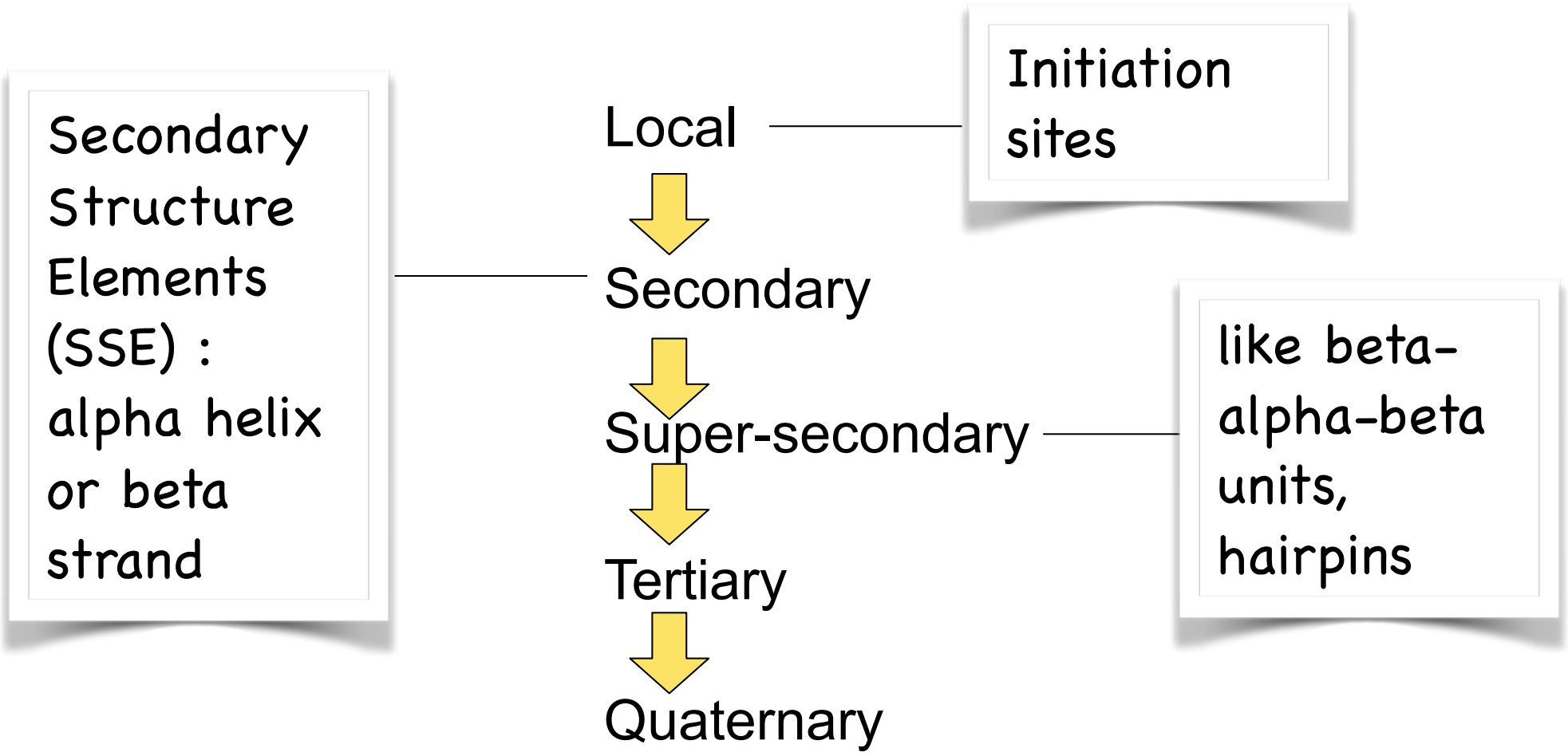
Many proteins share common core structures (Efimov cores)



Ancestral fold?  
and/or

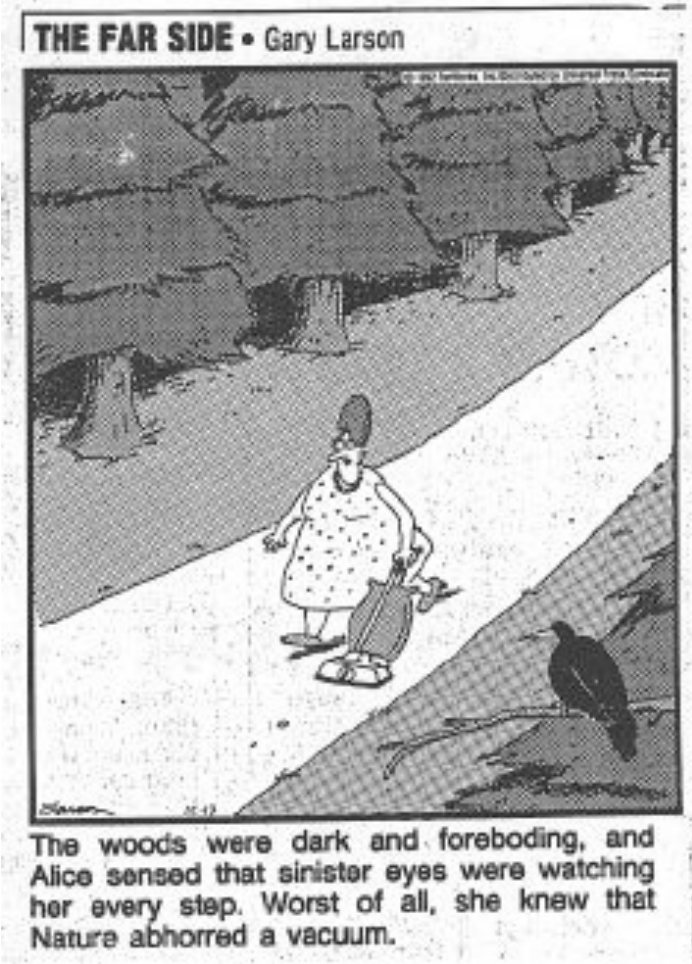
Folding intermediate?

# Folding



# Nature abhors a vacuum

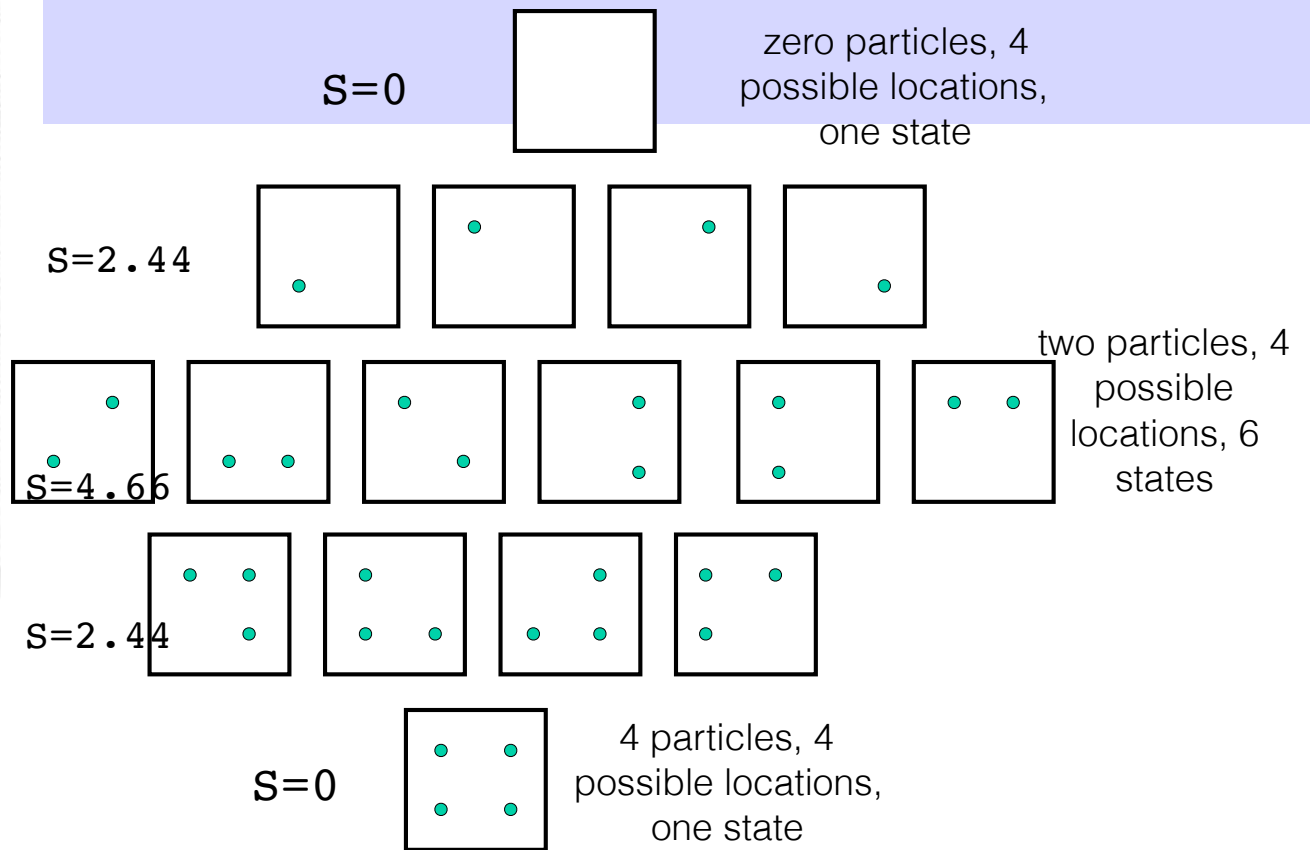
no, not this kind...



There is only **one way** to make space empty, but **many ways** to fill it.

$S = p \log p$ , where  $p$  is the number of states.

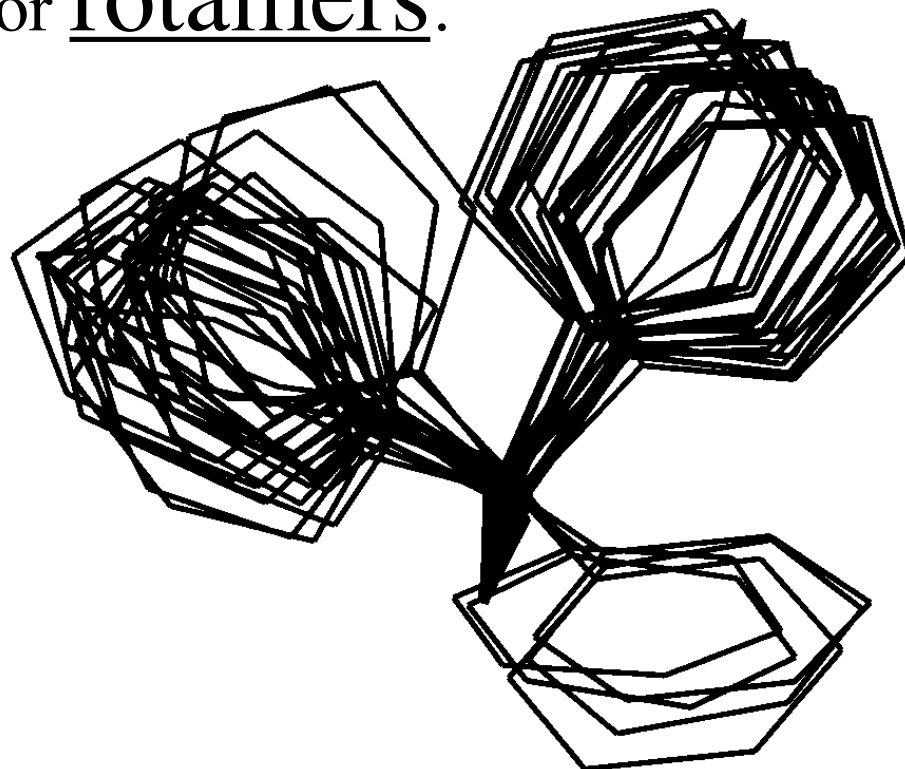
Higher entropy means more probable.



# Sidechain Rotamers

*Discrete approximation of the continuous space of backbone angles.*

Sidechain conformations fall into discrete classes called rotational isomers, or rotamers.



A random sampling of Phenylalanine sidechains, w/  
backbone superimposed